# Cost effective, computer-aided analytical performance evaluation of chromosomal microarrays for clinical laboratories 

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Goodman, Corey William. "Cost effective, computer-aided analytical performance evaluation of chromosomal microarrays for clinical laboratories." MS (Master of Science) thesis, University of lowa, 2012.
https://doi.org/10.17077/etd.u7hc7qb3

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# COST EFFECTIVE, COMPUTER-AIDED ANALYTICAL PERFORMANCE EVALUATION OF CHROMOSOMAL MICROARRAYS FOR CLINICAL LABORATORIES 

by<br>Corey William Goodman

# A thesis submitted in partial fulfillment of the requirements for the Master of Science degree in Electrical and Computer Engineering in the Graduate College of The University of Iowa 

July 2012

Thesis Supervisors: Professor Thomas L. Casavant Assistant Professor Benjamin W. Darbro

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## Graduate College

The University of Iowa
Iowa City, Iowa

## CERTIFICATE OF APPROVAL

MASTER'S THESIS

This is to certify that the Master's thesis of

Corey William Goodman
has been approved by the Examining Committee for the thesis requirement for the Master of Science degree in Electrical and Computer Engineering at the July 2012 graduation.

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To my grandfather, William Conrad Goodman who encouraged all his children and grandchildren to attend an institution of higher learning, despite lacking the opportunity to attend one himself.

## ACKNOWLEDGMENTS

I would like to thank Professor Thomas Casavant for his guidance and support for this project, as well as all of his guidance through much of my academic career. With regard to this project, I would like to especially thank Benjamin Darbro whose assistance has been invaluable. I would also like to thank Val Sheffield, Terry Braun, and John Robinson for serving on my thesis committee. Lastly, I would also like to thank my coworkers, family, and friends for their support and encouragement. All have helped make my time at the University of Iowa very meaningful and enjoyable.


#### Abstract

Many disorders found in humans are caused by abnormalities in DNA. Genetic testing of DNA provides a way for clinicians to identify disease-causing mutations in patients. Once patients with potentially disease-causing mutations are identified, they can be enrolled in treatment or preventative programs to improve the patients' long term quality of life. Array-based comparative genomic hybridization (aCGH) provides a highresolution, genome-wide method for detecting chromosomal abnormalities. Using computer software, chromosome abnormalities, or copy number variations (CNVs) can be identified from aCGH data. The development of a software tool to analyze the performance of CGH microarrays is of great benefit to clinical laboratories. Calibration of parameters used in aCGH software tools can maximize the performance of these arrays in a clinical setting. According to the American College of Medical Genetics, the validation of a clinical chromosomal microarray platform should be performed by testing a large number (200-300) of well-characterized cases, each with unique CNVs located throughout the genome. Because of the Clinical Laboratory Improvement Amendment of 1988 and the lack of an FDA approved whole genome chromosomal microarray platform the ultimate responsibility for validating the performance characteristics of this technology falls to the clinical laboratory performing the testing. To facilitate this task, we have established a computational analytical validation procedure for CGH microarrays that is comprehensive, efficient, and low cost. This validation uses a higher resolution microarray to validate a lower resolution microarray with a receiver operating characteristic (ROC)-based analysis. From the results we are able to estimate an optimal $\log _{2}$ threshold range for determining the presence or absence (calling) of CNVs.


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## CHAPTER 1

## INTRODUCTION

Chromosomal microarray (CMA) is a broad term often used to describe clinical testing for DNA copy number variation (CNV) utilizing either single nucleotide polymorphism (SNP) or comparative genomic hybridization microarrays (aCGH). CMA has proven to have a much higher diagnostic yield than conventional chromosome analysis or sub-telomeric fluorescence in situ hybridization (FISH) for a range of developmental phenotypes (Hochstenback, et al. 2009; Shen, et al. 2010; Vissers, et al. 2010). This increase in diagnostic yield is facilitated in part by the much higher resolution of microarray strategies in comparison to conventional cytogenetic techniques. It has been recommended that chromosomal microarrays be a first-tier diagnostic test for individuals with non-syndromic intellectual disability/developmental delay, autism spectrum disorders, or multiple congenital anomalies (Miller, et al. 2010; Manning and Hudgins 2010).

In this thesis, CGH-based microarray platforms were used for all CMA tests performed. With the improvements in resolution that come from array-based CGH (aCGH) methods, discoveries of many polymorphic CNVs have been found in healthy individuals as well as novel pathogenic CNVs. Polymorphic (common) CNVs are regions of DNA in which deletions and/or duplications normally occur in the population at a frequency higher than would be expected to occur at random. Typically, polymorphic CNVs are benign or have no known clinical significance. The presence of common, polymorphic CNVs found in the "normal" population makes detection of novel pathogenic CNVs difficult.

A disadvantage of aCGH can be the test-to-test variability. This can arise from a number of different factors including, variation in equipment used in the testing process,
the individuals performing the tests, different laboratory environments, or laboratory environmental factors over time and between tests (especially humidity, heat and ozone levels). Other artifact sources include differential labeling efficiency of dyes for the test and reference sample, uneven spotting of DNA to the microarray, variations in washing efficiency, and variations in scanning efficiency of the microarray. The resulting variability can be partially addressed using normalization techniques, but variability in data from laboratory to laboratory can still exist. In comparisons between different array platforms, different laboratories performing tests, and different algorithms for CNV calling, it has been found that variation remains a vexing problem. When taking into account both large and small CNVs, a comparison among algorithms using the same raw data typically yielded less than $50 \%$. It has also been demonstrated that the reproducibility of tests on many platforms was less than $70 \%$ (Pinto, et al. 2011).

Many algorithms used for calling CNVs have parameters, such as an intensity threshold or minimum length, that can be calibrated to each laboratory setting in order to optimize the performance of the tools. A software tool that can provide a general analytical calibration of parameters used in CNV calling algorithms can be of great use to clinical laboratories. No such tool is currently known to exist and would greatly enhance the diagnostic accuracy of this important clinical test.

Recently, the American College of Medical Genetics (ACMG) published new guidelines for the interpretation and reporting of constitutional CNVs as well as recommendations for the design and performance expectations of the microarrays used in clinical CMA testing (Kearney, South, et al. 2011; Kearney, Thorland, et al. 2011). Recommendations for microarray design and validation include the ability to detect genome-wide CNVs of at least 400 Kb in size at $99 \%$ analytical sensitivity (with a lower limit of the $95 \%$ confidence interval $>98 \%$ ) and a false-positive rate of $<1 \%$ (Kearney, South, et al. 2011). The ACMG places the task of this analytical validation on the array
manufacturers; however, in the absence of a manufacturer providing this data, it is ultimately the clinical laboratories' responsibility to validate the performance of these arrays, as there is still no FDA-approved, in-vitro diagnostic whole-genome chromosomal microarray platform or test kit.

According to the ACMG, the validation of a clinical chromosomal microarray should be performed by testing a sufficiently large number (200-300) of wellcharacterized cases that contain a collection of appropriately sized (majority being $<1 \mathrm{Mb}$ ), unique CNVs that are located throughout the genome. This is a difficult standard to meet for many clinical laboratories. Even with a diagnostic yield of $\sim 15-20 \%$, a clinical laboratory would have to test $>1000$ patients to naturally accumulate this many cases with diagnostic CNVs, and this does not account for factors such as recurrent CNVs or an uneven distribution across the genome.

In the research for this thesis a computer-aided receiver operator characteristic (ROC) based method has been developed that clinical laboratories can use to determine their own CMA platform analytical sensitivity and false positive rate. This method can utilize both novel and common/polymorphic CNVs with a per-probe approach (as opposed to per-CNV) to quantify outcome metrics such as true and false positive and negative results as well as sensitivity and specificity in general. The method developed can also be used to perform calibration of parameters used in algorithms that detect CNVs in aCGH data. Using two microarray designs that differ in their level of resolution it is shown that an analytical evaluation can be performed with as few as 20 cases in total.

CMA testing influences management of patients in many ways including generation of medical referrals, and providing guidance for diagnostic imaging and specific laboratory testing (Coulter, et al. 2011). Given the complexity of CMA testing and the implications it holds for future patient management, establishment of quality control and performance metrics is of utmost importance. Even if manufacturers of
chromosomal microarrays have performed extensive quality controls, it is still necessary for individual laboratories to verify these performance characteristics in their own setting and with their distinct patient populations. Thus, the establishment of a validation procedure for CMAs that is both comprehensive and low cost is of great significance to the clinical laboratory community.

## CHAPTER 2

## BACKGROUND

### 2.1 Array-Based Comparative Genomic Hybridization (aCGH)

Although the methods presented here can be applied to data from any chromosomal microarray with oligonucleotide probes, in this project the type of chromosomal microarray used was a comparative genomic hybridization array (array CGH or aCGH). Array-based comparative genomic hybridization is a method used to detect chromosomal anomalies on a genome-wide, high-resolution scale. An overview of the aCGH process is outlined in Figure 2.1 (Theisen 2008).


Figure 2.1: A diagram outlining the process of array-based comparative genomic hybridization. Used with permission

### 2.1.1 CGH Microarrays

Array CGH achieves a high testing resolution by using a substrate (e.g., a glass slide) with many small strands of single-stranded target DNA (oligonucleotides) attached to the substrate. These small amounts of DNA (commonly referred to as probes) are arranged into spots and immobilized onto a glass slide. The probes vary in length from small oligonucleotides of less than 50 base pairs (also referred to as mer) to large regions hundreds of thousands of base pairs long (commonly referred to as BACs). Probes are arranged in a way to prevent poor performance of a region of the microarray to affect the whole test. This is done by attempting to prevent probes found close together on the genome from being placed close together on the array. The length of the probes and the genomic distance between the probes determines the resolution of each array (Theisen 2008). It is not necessary that genomic locations of probes in a lower resolution microarray be a subset of probes in a higher resolution microarray. The primary array platforms used in this project were from the manufacturer Roche NimbleGen and are described in Table 2.1 (Roche NimbleGen n.d.).

Table 2.1: Details of Roche NimbleGen microarrays that were used for this project.

| Array Description | Probe Length | Median Probe Spacing |
| :---: | :---: | :---: |
| Human CGH 385K Whole-Genome Tiling v2.0 Array | 60 mer | 7073 bp |
| Human CGH 720K Whole-Genome Tiling v3.0 Array | 60 mer | 2509 bp |
| Human CGH 2.1M Whole-Genome Tiling v2.0D Array | 60 mer | 1169 bp |

### 2.1.2 Probe Hybridization

When a CMA test is performed, DNA is extracted from a sample of interest, or test sample, and labeled with a fluorescent dye with specific chromatic spectral characteristics (in most applications this is typically displayed as green as it is a reflection of the Cy3 dye used). A sample of DNA that is considered normal is used as a control/reference sample and labeled with a fluorescent dye differing in color from the sample of interest, typically red (Cy5 dye). The two samples are denatured into singlestranded DNA, mixed together, and then applied to the microarray. The single-stranded DNA from the test and reference samples will then be allowed to hybridize to probes matching their complementary sequence. The result will be regions with different levels of intensities between the two fluorescent dyes (Theisen 2008).

### 2.1.3 Probe Intensities

These levels of intensity between the two dyes provide a means for estimating the copy number of the test genome compared to the reference genome. For example, if a test sample was labeled with a green fluorescent dye and a reference sample was labeled with a red fluorescent dye, samples of equal copy number would appear yellow in color because spots on the microarray would have roughly equal amounts of each sample hybridizing to the probe for that region. Spots appearing green would indicate a higher copy number for that region in the test genome because more DNA from the test DNA hybridized to the probe for the region than reference DNA. Spots appearing red would indicate a lower copy number for that region in the test genome because less DNA from the test DNA hybridized to the probe for the region than reference DNA. Finally probes that appear black would indicate that no hybridization occurred for either sample in that region. Figure 2.2 illustrates a typical two-color microarray (Chen n.d.).


Figure 2.2: An example image of a microarray. The spots on this image show a range of fluorescent intensities between the test and reference sample.

### 2.1.4 $\log _{2}$ Ratios

A highly sensitive ultraviolet (UV) spectral scanner reads the intensities of each color on each spot on the microarray. Regions that show an increase in copy number by a factor of two will have a test/control ratio of 2 . Genes that show a decrease in copy number by a factor of two will have a test/control ratio of 0.5 . Because there is a difference in how the experiment treats gained versus lost regions on the microarray, intensities of green to red dyes are normalized with a base two logarithmic transformation (known as $\log _{2}$ ratio). This centers regions that have an equal test/control ratio of 1 to a $\log _{2}$ ratio of 0 . Regions gained by a factor of two will have a $\log _{2}$ ratio of 1 and regions with a loss equivalent to a factor of two will have a $\log _{2}$ ratio of -1 . In this thesis, when the value a $\log _{2}$ ratio threshold is mentioned, it is implied that it be negative for deletions and positive for duplications.

### 2.1.5 Normalization

Other normalization adjustments are made to the microarray data as a whole so that meaningful information can be found (Quackenbush 2002). In general normalization techniques consist of background correction, transformation (e.g. $\log _{2}$ ratio transformation described above), and rescaling. Some normalization techniques used on microarrays are: scale normalization, locally weighted scatterplot smoothing (LOWESS), quantile normalization, and variance stabilization and normalization (VSN). The LOWESS is a technique based on linear regression and is the most common type of normalization performed for two color microarrays (Beissbarth, et al. 2005). The underlying normalization technique should not have any unexpected influence on the algorithms developed for this thesis.


Sample: 228557_385k_Patient1_segMNT
Figure 2.3: A genome wide view of $\log _{2}$ data for a patient. The $y$-axis shows the normalized $\log _{2}$ ratio data and the x -axis shows genomic position grouped by chromosome in increasing order. From this image it can be determined that the test sample used was a male and the reference sample used was a female. This can be seen in the X and Y chromosomes where the entire X chromosome appears to exhibit a decrease in copy number and the entire $Y$ chromosome appears to exhibit a increase in copy number. The green and red lines indicate low and high copy number variations. This image was generated with Nexus Copy Number ${ }^{\mathrm{TM}}$ software licensed by Shivanand R. Patil Cytogenetics and Molecular Laboratory at the University of Iowa.

### 2.1.6 Copy Number Detection

There are many CNV calling algorithms that can be used to detect copy number variations in aCGH data (Venkatraman and Olshen 2007; Marioni, Thorne and Tavaré 2006; Zhang and Gerstein 2010). Many of these algorithms are specific to a certain type of microarray. The specific algorithm used for testing in this research was the FASST algorithm, which is part of the BioDiscovery Nexus Copy Number ${ }^{\mathrm{TM}}$ software. The FASST algorithm uses a Hidden Markov Model (HMM) approach that estimates possible segment levels that may occur between expected states (BioDiscovery 2011). The segments whose mean $\log _{2}$ ratios exceed a specified threshold are called as copy number variations.


Figure 2.4: A diagram showing how the FASST algorithm could analyze aCGH data. The data are segmented and then segments classified as CNVs if they exceed a defined threshold. In this diagram the red and green lines signify deletion and duplication threshold respectively. Circled segments indicate segments that would be classified as deletions or duplications based on the shown threshold. Segments shown here have been fabricated to provide a visual demonstration of the aCGH CNV calling process.

### 2.2 Previous Work

This work builds upon a previously developed CNV-calling algorithm -CGHTool. Finding small novel CNVs in aCGH data is challenging. The goal of CGHTool was to provide an algorithm that could detect small CNVs with high confidence. The CGHTool program creates a background file consisting of aCGH data from many patients (several hundred). From this it calculates an average and standard deviation of the data for each oligonucleotide probe on the CGH microarray. In general, a region of the genome can be classified (i.e., called) a CNVs if the number in the region exceed a multiple of the standard deviation in the same direction (gain or loss). While working on this algorithm, it was found that there was a need to calibrate several of the algorithms parameter. Among these was one essential metric: the base two logarithmically transformed signaling intensity ratio; hereafter referred to simplay as the $\log _{2}$ ratio. This ratio is taken between the measured intensity in a patient (unknown) sample and a control sample.

There have been several publications that have sought to prove the effectiveness of chromosomal microarrays and provide a strategy for clinical validation. Each publication has emphasized the need for validation of aCGH methods (Shaffer, et al. 2007; Shen and $\mathrm{Wu}, 2009$; Yu, et al. 2009). It has been hypothesized that performance of specificity will increase when more consecutive probes are used when analyzing CNVs. There are a large number of benign and unknown CNVs that may contribute to poorer performance of microarrays. It is hypothesized that the majority of unknown CNVs are benign and as more known benign CNVs are discovered, arrays may be redesigned to improve performance (Shen and Wu, 2009). Currently, there has been no method provided that calculates true or false negatives using aCGH data. Since the calculations
of sensitivity and specificity rely on true and false negatives, these metrics are required to adhere to the guidelines set out by the ACMG.

### 2.2.1 Fluorescence in Situ Hybridization (FISH) Validation

Fluorescence in situ hybridization (FISH) is a technique used to detect DNA sequences. This technique first involves creating a fluorescent DNA probe compliment to a sequence of interest. The probe and target DNA are denatured and then combined so the probe may hybridize to its complement on the target DNA. This allows for visualization of the target sequence on the chromosome (O'Connor 2008). FISH can be used as an alternative technology for finding CNVs. Verification of aCGH can be done with FISH also, but it is a labor intensive and costly process as FISH can only interrogate one chromosomal region at a time (Balif, et al. 2007). A computational-based method that could provide validation of aCGH data could be very useful.

### 2.3 Receiver Operating Characteristic (ROC)

Receiver operating characteristic (ROC) curves were developed in World War II to improve signal to noise detection in radar signals (Krzanowski and Hand 2009). Since World War II, ROC analysis has become commonly used for evaluation of clinical diagnostic tests (Zou, O'Mally and Mauri 2007). A ROC analysis measures the costs and benefits of the changing prediction parameters using sensitivity and specificity. The approach taken in this research was to perform an analytical validation of aCGH data using a ROC-based method. A receiver operating characteristic or ROC is the plot of true positive rate (sensitivity) versus false positive rate (1-specificity) for a changing
parameter. The false positive rate (FPR) is plotted along the x -axis while sensitivity is plotted along the $y$-axis. Each axis is on a scale of 0 to 1 .

### 2.3.1 Sensitivity and Specificity

Sensitivity and specificity are statistical measures of a binary classifier's performance. To calculate the sensitivity and specificity the classifier must be compared to a gold standard set. In a binary classifier, there are four outcomes possible. True positives (TP) occur when a result classified as positive matches the gold standard set. False positives (FP) occur when a result classified as positive does not match the gold standard set. True negatives (TN) occur when a result classified as negative matches the gold standard set. False negatives (FN) occur when a result classified as negative does not match the gold standard set. Even if a classifier is not binary (e.g. duplication, deletion, or no variation), the classifier can be made to emulate a binary classifier. This can be done by combining results (e.g. deletions or duplications) and classifying them as being positive and combining all other results (e.g. no variation) and classifying them as being negative.

The sensitivity is a measure from 0 to 1 of how well a classifier can identify positive results. The optimal measure for this statistic would be 1 , meaning that no results that are negative are classified as positive by the gold standard set. The calculation of sensitivity using the outcome of classifier results compared to a gold standard set is shown below in Equation 2.1.

Equation 2.1: Measure of sensitivity for a classifier

$$
\text { Sensitivity }=\frac{\text { True Positives }}{\text { True Positives }+ \text { False Negatives }}
$$

The specificity is also a measure from 0 to 1 , but measures how well a classifier can identify negative results. The optimal measure for this statistic would also be 1 , meaning that no results that are positive are classified as negative by the gold standard set. The false positive rate is a measure of 1 - specificity giving it an optimal value of 0 . The calculation of specificity using the outcome of classifier results compared to a gold standard set is shown below in Equation 2.2.

Equation 2.2: Measure of specificity for a classifier

$$
\text { Specificity }=\frac{\text { True Negatives }}{\text { True Negatives }+ \text { False Positives }}
$$

### 2.3.2 Confidence Intervals

A confidence interval is used to determine the reliability of an estimate. Confidence intervals can be used with performance metrics such as sensitivity and specificity. For this research the confidence intervals used were calculated according to the efficient-score method (Newcombe 1998). When calculating a confidence interval, the efficient-score method accounts for the bounds of sensitivity (0 to 1 ) and FPR ( 0 to 1).

### 2.3.3 Receiver Operator Characteristic Plot

A ROC plot is created by running several tests with a classifier while varying a parameter used in a classifier (e.g. $\log _{2}$ ratio threshold). Each of the tests results in a point on the plot of FPR versus sensitivity. The points form a curve that allows visualization of the trade-offs between FPR and sensitivity for the changing classifier
parameters. For a ROC curve the optimal point would be $(0,1)$ with all results classified correctly. This outcome is rarely the case so an optimal point can be chosen based on desired results of classifier sensitivity and specificity. A general ROC plot is shown in Figure 2.5 (de Vet, et al. 2007).


Figure 2.5: A plot of a receiver operating characteristic curve.

## CHAPTER 3

## APPROACH

The goal of the research for this thesis was to use a computer-aided approach to appropriately validate the performance characteristics of a whole-genome chromosomal microarray. To do this, two microarray platform designs were used that differed primarily in their level of resolution (i.e., number of unique probes), where the higher resolution CNVs were used as a "gold standard" set. This is similar to using a higher resolution photograph to validate a lower resolution photograph. With greater detail comes the ability to recognize patterns with more confidence. The two main platforms used in the validation were the NimbleGen 720,000 (720K array) and the NimbleGen 385,000 (385K array) microarrays. An additional validation was performed comparing the 385 K array to a NimbleGen $2,100,000$ ( 2.1 M array) microarray in which similar results were found. Results of the analyses can be found in Appendix A. All analyses were performed using CNVs greater than 100 Kb and CNVs greater than 400 Kb . The minimum size of 100 Kb was estimated to be the smallest CNV size that could be confidentially detected using a 385 K array. The 400 Kb minimum CNV size cutoff was used to adhere to the guidelines of the ACMG.

## 3.1

### 3.2 Validation Samples

Twenty samples were used for validation comparisons. All cases were previously analyzed and interpreted by standard clinical criteria. The set of samples included both
normal (no known pathogenic CNVs) and abnormal cases in which a known pathogenic lesion was identified (i.e. 17 q 12 or 22q11.2 deletion). An appropriate mix of male and female patients, as well as small $(100-400 \mathrm{~Kb})$ and large $(>400 \mathrm{~Kb})$ duplications and deletions were present. The CNVs present in these cases covered a significant portion of the genome (Table 3.1). Additionally, each case contained between 10 and 40 common, polymorphic CNVs.

Table 3.1: Genome wide aCGH probe coverage of CNV calls represented as probes, base pairs, percentage of probes, and percentage of genome covered.

| Type of CNV | Total Number of Probes Contained in CNVs |  | \% of Total Probes on the Array Contained in CNVs |  |  | \% of Genome Covered by Probes Contained in CNVs |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Per Patient | Total | Per Patient | Total |  | Per Patient | Total |
| 385 K (Calls > 100 Kb ) | 472 | 9,442 | 0.12236\% | 2.44729\% | 81,475,048 | 0.12730\% | 2.54610\% |
| 385 K (Calls > 400Kb) | 210 | 4,209 | 0.05455\% | 1.09094\% | 37,969,898 | 0.05933\% | 1.18656\% |
| 720K (All CNV Calls) | 799 | 15,970 | 0.11095\% | 2.21901\% | 95,958,945 | 0.14994\% | 2.99872\% |

Note: Numbers shown are for CNV calls for a combination of all 20 samples. CNV calls used in the analysis were made using the FASST algorithm in Nexus Copy Number with a $\log _{2}$ ratio of 0.30 for both the 385 K and 720 K arrays.

### 3.3 Manual CNV-Based Validation

A manual CNV-based validation was performed using the FASST algorithm in Nexus Copy Number ${ }^{\text {TM }}$ to call CNVs on two different array platforms, a higher resolution NimbleGen 720K array and a lower resolution NimbleGen 385K array. A $\log _{2}$ ratio threshold of 0.3 was used for calling CNVs for both platforms. The higher resolution arrays were used as a gold standard set for the lower resolution arrays. CNVs on the lower resolution arrays were compared to the higher resolution arrays to assess
false positives, true positives, false negatives, and true negatives. When comparing arrays, true negatives were defined as those intervening regions between CNVs of greater than 100 Kb on the higher resolution array that had no corresponding CNV regions on the lower resolution array. Analyses were performed using a CNV size threshold of 100 Kb and 400 Kb as well as for both benign and clinically significant CNVs together and for clinically significant CNVs alone.

Aside from the laborious nature of this type of manual analysis it is clear that with a per-CNV based analysis and this few cases there are not enough CNV to truly establish precise and meaningful sensitivity and specificity measures. When examining only clinically significant CNVs greater than 400 Kb only 18 CNVs were available for analysis. Because of the extensive time and effort involved in performing this manual comparison only one $\log _{2}$ ratio threshold could be examined for each array type precluding any analysis that might identify a different $\log _{2}$ ratio threshold that would further increase sensitivity without a significant loss in specificity (or vice versa) via ROC analysis. It was clear that a computer-aided approach was needed to appropriately validate the performance characteristics of a whole-genome chromosomal microarray for varying $\log _{2}$ ratios.

### 3.4 Analysis of Array Metrics

As part of our computer-aided validation, we sought to determine which array metric(s) would be most appropriate on which to base future ROC analysis. We did this by creating a (Perl) software tool to compare the CNV calls from the lower resolution arrays to the CNV calls from the higher resolution arrays. All CNV calls were produced by using the FASST algorithm from Nexus Copy Number ${ }^{\text {TM }}$. The higher resolution arrays were again treated as a "gold standard" to which the lower resolution array data
were then compared. A previously FISH-validated threshold $\log _{2}$ ratio value of 0.3 was used for the FASST algorithm when calling the CNVs for both array platforms. The analysis, like the manual validation, was performed twice for all CNV calls of 100 Kb or greater and all CNV calls of 400 Kb or greater. For each experiment, every CNV called from the lower resolution arrays was checked for any overlapping CNV calls from the higher resolution arrays. From this, two sets of lower resolution CNVs could be made for each size-cutoff experiment, one set that had one or more overlapping higher resolution CNVs (true positives) and one set that had no overlapping higher resolution CNVs (false positives).

The CNVs within each set were examined by looking at the $\log _{2}$ ratios, CNV sizes in base pairs, and number of probes in each CNV. The median and mean values of each of these CNV metrics were calculated. By comparing these metrics in the two sets of CNVs for each experiment, we were able to perform an unpaired $t$-test for groups of unequal size and variance to determine if the metrics for the two sets differed significantly. We could then choose metrics that were statistically significant for use in our validation techniques.

### 3.5 Computer-Aided Probe-Based Validation

Once a significant parameter was found, the next goal was to find the optimal $\log _{2}$ ratio that could be used to call CNVs and maximize both sensitivity and specificity. This optimal $\log _{2}$ ratio could be calculated from a ROC analysis, which plots the sensitivity vs. false positive rate as the threshold of an experimental metric is varied. The $\log _{2}$ ratio threshold used to call CNVs in the aCGH data was found to be the most significant experimental metric. The results section gives justification for this decision.

Whereas the analysis could be performed on a per-CNV basis, as with the manual analysis, the number of CNVs would be the same and still lacking in ability to calculate meaningful performance metrics. This led to the use of a novel per-probe approach that compared probes in CNV calls from the lower resolution array to calls from the higher resolution array and assigned the probes of the lower resolution array "truth-values" based on corresponding locations in the higher resolution array. The CNV calling algorithm was run with varying $\log _{2}$ ratio thresholds to create many different sets of CNV calls for both the lower resolution arrays and the higher resolution arrays.

### 3.5.1 CNV Validation Sizes

To make the validation applicable to the guidelines of the ACMG, all CNV calls used in the lower resolution arrays had to be greater than 400 Kb . Similarly, only CNVs in the higher resolution array greater than 400 Kb could have probes counted as false positives if no corresponding CNVs in the lower resolution array existed. As not to penalize the arrays for performing better than ACMG expectations, smaller CNVs called on both lower and higher resolution arrays could be used to validate corresponding larger ( $>400 \mathrm{~Kb}$ ) CNVs on the opposite array. This approach allowed probes in larger ( $>400 \mathrm{~Kb}$ ) CNVs to be validated as true positives if smaller CNVs were called in the same region, but would not penalize the arrays with false positives and false negatives.

### 3.5.2 Probe Validation Range

Because it is not necessarily the case that the probes in the lower resolution array are a subset of the probes in the higher resolution array, each probe in the lower resolution array was validated by probes in the higher resolution array within a certain
genomic distance. In tests performed on correlation between genomic locations of probes in the 385 K array and 720 K array, it was found that only $17 \%$ of the probes in the 385 K array had a corresponding probe found in the exact same genomic location on the 720 K array. For all tests performed using the NimbleGen 385K array the genomic distance in which higher resolution array probes could validate a 385 K array probe was 15 Kb . This distance was chosen because the median probe spacing for the 385 K array was 7 Kb to 8 Kb . Because lower resolution array probes could be validated by a range of higher resolution array probes, all lower resolution array probes that did not have a higher resolution array probe with the genomic distance validation range were excluded from the analysis.

### 3.5.3 ROC Analysis

Because of the variability between CNV calls for different $\log _{2}$ ratio thresholds, in the ROC analysis a single higher resolution $\log _{2}$ ratio set of CNV s was used as a gold standard while each lower resolution $\log _{2}$ ratio set of CNVs was compared to the gold standard. This analysis was run for every set of higher resolution $\log _{2}$ ratio set of CNVs. A ROC plot was generated for every higher resolution $\log _{2}$ ratio gold standard used. Each ROC plot contained a comparison of each of the lower resolution $\log _{2}$ ratios to a single higher resolution $\log _{2}$ ratio gold standard set.

When performing each comparison in the ROC analysis all probes in the lower resolution arrays and higher resolution arrays were labeled as either a CNV (deletion or duplication) or normal (not a CNV) according to the $\log _{2}$ ratio thresholds being compared. For each $\log _{2}$ ratio threshold tested against the gold standard, all lower resolution array probes for each sample were assigned a truth-value. The truth-value for each lower resolution array probe was assigned as a true-positive or true-negative if one
of the higher resolution array probes in its coverage range $(15 \mathrm{~Kb})$ had the same outcome (gain, loss, normal/no CNV), otherwise the lower resolution array probe was labeled as a false-positive or false-negative. A flow diagram of the analysis pipeline is shown in Figure 3.1.


Figure 3.1: A Demonstration of a probe based ROC analysis performed using arrays of different resolution.

### 3.5.4 Variations of Analysis

In addition to varying the gold standard $\log _{2}$ ratio threshold used for the ROC analyses, the types of CNVs used in the analyses was also varied. There were three types of analyses performed: just for copy number gains, just for copy number losses, and for a combination of copy number gains and losses.

Another variation of the analysis allowed for exclusion of probes found in common, polymorphic regions. There were 158 of these common regions found where each region occurred in at least $5 \%$ of the patient population used in the dataset. Common CNVs were defined by their presence in HapMap samples as ascertained by Conrad and colleagues (Conrad, et al. 2010). These common regions contain clinically benign CNVs, so these regions were excluded in the hope of improving the performance of the analysis.

### 3.5.5 Optimal Experimental Metrics

Once ROC curves were created, they were utilized to determine the optimal $\log _{2}$ ratio threshold used for the experiment. The optimal points on each curve should provide the best trade off between sensitivity and false positive rate. Two methods for determining this metric were formed. The first method calculated the optimal point by using linear distance. A perfect classifier would perform with $100 \%$ specificity and a $0 \%$ false positive rate, or be a point at $(0,1)$ on the ROC plot. Using a linear method, the optimal point would be the closest point to $(0,1)$ on the plot. Because sensitivity and false positive rate did not always reach 1, the ROC plots were normalized to the maximum sensitivity and false positive rate before calculating the optimal $\log _{2}$ ratio (closest linear distance to $(0,1)$ ). The second approach to calculate the optimal point was
to take the derivative of the ROC curve to find the maximum change in slope. This approach did not perform as consistently as our linear-distance approach because the rate of change for the curve was not consistent for all analyses. A demonstration of how the optimal point is calculated using a linear-distance approach can be seen in Figure 3.2 and Table 3.2.


Figure 3.2: A demonstration of how the optimal point is determined based on a normalized ROC plot.

Table 3.2: An example of a computer-aided single $\log _{2}$ ratio threshold comparison of two different array resolution designs.

| 720K Log <br> Ratio | 385K Log <br> $\mathbf{2}$ <br> Ratio | FPR | Sensitivity | Normalized Optimal Distance |
| :---: | :---: | :---: | :---: | :---: |
| 0.40 | 0.20 | 0.04982 | 0.99864 | 1.00000 |
| 0.40 | 0.25 | 0.02321 | 0.99804 | 0.46592 |
| 0.40 | 0.30 | 0.01090 | 0.98462 | 0.21927 |
| $\mathbf{0 . 4 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 0 0 4 1 4}$ | $\mathbf{0 . 9 5 6 3 6}$ | $\mathbf{0 . 0 9 3 2 1}$ |
| 0.40 | 0.40 | 0.00354 | 0.93152 | 0.09775 |
| 0.40 | 0.45 | 0.00265 | 0.76560 | 0.23933 |
| 0.40 | 0.50 | 0.00157 | 0.64768 | 0.35285 |
| 0.40 | 0.55 | 0.00082 | 0.53029 | 0.46928 |
| 0.40 | 0.60 | 0.00071 | 0.44948 | 0.55009 |
| 0.40 | 0.65 | 0.00042 | 0.39108 | 0.60845 |
| 0.40 | 0.70 | 0.00023 | 0.17975 | 0.82001 |

Note: Numbers correspond to the data points shown in Figure 3.2. The bolded row indicates the optimal $\log _{2}$ ratio found based on the closest linear distance (greyed box).

Whereas this analysis was capable of elucidating the optimal $\log _{2}$ ratio value to use to maximize sensitivity and specificity, the values obtained for specificity were clearly biased toward the very large number of true negative probes (non-CNV probes) present in the array comparisons. This resulted in specificities that routinely exceeded $99.999 \%$ across most $385 \mathrm{~K} \log _{2}$ ratios thresholds tested. To better calculate the specificity, we took the number of TN probes and divided it by the average number of probes present in $\mathrm{CNVs}>400 \mathrm{~Kb}$. This was deemed appropriate given that a requirement for any true or false positive probe was inclusion within a CNV that was $>400 \mathrm{~Kb}$.

### 3.5.6 Computational Analysis Design

A Perl script was developed to accurately compute the results of a ROC analysis given a paired set of CNV calls from raw microarray data. Using a duplicate set of 385 K
array and 720 K array data for 20 patients and 11 different $\log _{2}$ ratio thresholds, this could be performed on a typical desktop workstation in approximately 2 hours with an approximate memory footprint of 2GB. The Perl script developed (shown in Appendix B.1) allows a general input of aCGH probes genomic locations as well as a call type (copy gain/copy loss) paired with a general genomic start and stop position for CNVs. Because of this general input format performance of many different array platforms may be assessed. The Perl script also allows customizations described previously to be set using flags. For example the buffer range and minimum CNV size may both be customized. Other parameters such as inclusion or exclusion of common CNV regions may be set, as well as types of CNVs included in the analysis (duplications, deletions, or both).

A second Perl script was developed to combine the results of many higher resolution gold standard $\log _{2}$ ratios into one Microsoft Excel workbook with many worksheets. This script was created separately from the ROC analysis script because of it's dependencies on a 3rd-party Perl module Excel::Writer::XLSX (McNamara 2011). The script will read the standard output directory from the previous ROC analysis script and compile all the results into one Microsoft Excel workbook. Each analysis is shown in its own worksheet with optimal metrics calculated and a ROC plot generated. The script has options to adjust the false positive rate in way described previously.

### 3.6 Computer-Aided Region-Based Validation

It was thought that the FPR may be better represented if the ROC analysis were done for regions instead of probes, however, conducting region-based analyses proved challenging due to the incomplete classification of non-CNV regions with a truth value. The arrays could be quantified into CNV regions and non-CNV regions, but
precise classification of the regions proved difficult. For example, it is possible to classify a lower resolution CNV region based on the corresponding higher resolution regions. However, this was difficult due to the fact that not all regions were of a uniform size and regions from the different array types did not often correlate well with each other. The most intuitive way to classify these regions was to determine if a defined percentage of a given lower resolution region overlapped a similar higher resolution region.

One problem with this approach was that very large non-CNV (>> 400 Kb) regions in a lower resolution array may have an overlapping higher resolution CNV region that is in total a small percentage of the lower resolution, non-CNV region. If the majority of a lower resolution, non-CNV region is overlapped by higher resolution nonCNV regions it would be classified as a true negative, despite the fact that there existed a clear false negative region. This is just one of the cases contributing to the difficulty of classifying CNV calls, especially true negatives, with truth-values as regions of the genome. Using a probe-based analysis provided a roughly uniform spacing and coverage between differing array types, which made it easier to assign truth-values to the probes.

## CHAPTER 4

## RESULTS

### 4.1 Manual Validation Results

Based on the results of the manual validation of twenty cases a sensitivity of $79.8 \%$ (with a lower limit of the $95 \%$ confidence interval of $74.4 \%$ ) was achievable when using data from all CNVs (benign and clinically significant) greater than 100 Kb and a single $\log _{2}$ ratio threshold of 0.3 . For all CNVs greater than 400 Kb a sensitivity of $80.9 \%$ (with a lower limit of the $95 \%$ confidence interval of $66.3 \%$ ) and specificity of $99.2 \%$ (false positive rate of $0.8 \%$ with a higher limit of the $95 \%$ confidence interval of $2.2 \%$ ) was achievable. When examining only those CNVs $>400 \mathrm{~Kb}$ and clinically significant (known pathogenic lesions and novel CNVs of unclear clinical significance) a sensitivity of $100 \%$ and a specificity of $100 \%$ (false positive rate of $0 \%$ ) were achieved.

Even though the sensitivity and specificity were each $100 \%$, the $95 \%$ confidence intervals were quite large (sensitivity with a lower limit of the $95 \%$ confidence interval of $78.1 \%$ and specificity with a lower limit of the $95 \%$ confidence interval of $99.0 \%$ ). An example of the analysis performed for each case is represented in Table 4.1.

Table 4.1: Example case assessed by manual validation using two different array resolution designs.

| CNV <br> Location | $\begin{gathered} \hline \text { Size }(\mathrm{Kb}) \\ 385 \mathrm{~K} \\ \hline \end{gathered}$ | $\begin{gathered} \hline \text { Size }(\mathrm{Kb}) \\ 720 \mathrm{~K} \\ \hline \end{gathered}$ | $\begin{gathered} \hline \mathrm{Log}_{2} \text { Ratio } \\ 385 \mathrm{~K} \\ \hline \end{gathered}$ | $\begin{gathered} \mathrm{Log}_{2} \text { Ratio } \\ 720 \mathrm{~K} \\ \hline \end{gathered}$ | $\begin{gathered} \text { Truth Value } \\ (>100 \mathrm{~Kb}) \\ \hline \end{gathered}$ | $\begin{gathered} \text { Truth Value } \\ (>400 \mathrm{~Kb}) \\ \hline \end{gathered}$ | CNV Interpretation |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1p36.33 | 615 | [264] | -0.37 | [-0.28] | False Positive | False Positive | Benign |
| 1p36.11 | 168 | 140 | -0.552 | -0.569 | True Positive | Size Exclusion | Benign |
| 1p21.1 | 177 | 112 | -0.437 | -0.388 | True Positive | Size Exclusion | Benign |
| 1p13.3 | NA | 73 | NA | 0.344 | Size Exclusion | Size Exclusion | Benign |
| 1q23.3 | 176 | [162] | 0.303 | [0.22] | False Positive | Size Exclusion | Benign |
| 1q44 | NA | 43 | NA | 0.708 | Size Exclusion | Size Exclusion | Benign |
| 2p11.2 | 517 | 214 | 0.337 | 0.346 | True Positive | True Positive | Benign |
| 2p11.2 | 139 | 78 | -0.527 | -0.339 | True Positive | Size Exclusion | Benign |
| 2q13 | [640] | 358 | [0.28] | 0.304 | False Negative | Size Exclusion | Benign |
| 6p25.3 | [145] | 97 | [0.29] | 0.331 | Size Exclusion | Size Exclusion | Benign |
| 6p22.1 | NA | 30 | NA | 0.442 | Size Exclusion | Size Exclusion | VUCS |
| 7p14.1 | NA | 40 | NA | 0.334 | Size Exclusion | Size Exclusion | VUCS |
| 7q35 | 153 | NA | -0.302 | NA | False Positive | Size Exclusion | Benign |
| $\begin{gathered} 8 \mathrm{p} 23.2 \mathrm{p} 2 \\ 3.1 \end{gathered}$ | 517 | 520 | 0.466 | 0.497 | True Positive | True Positive | VUCS |
| 8p23.1 | 76 | 53 | 0.609 | 0.906 | Size Exclusion | Size Exclusion | Benign |
| 11p15.4 | NA | 95 | NA | 0.403 | Size Exclusion | Size Exclusion | Benign |
| 14 q 11.2 | 324 | 166 | 0.363 | 0.35 | True Positive | Size Exclusion | Benign |
| 14q11.2 | 120 | NA | 0.315 | NA | False Positive | Size Exclusion | Benign |
| 15q11.2 | NA | 439 | NA | -0.421 | False Negative | False Negative | Benign |
| $\begin{gathered} 16 \mathrm{p} 13.3 \mathrm{p} \\ 13.2 \\ \hline \end{gathered}$ | 545 | 546 | -0.724 | -0.84 | True Positive | True Positive | VUCS |
| 17 q 21.31 | 148 | 110 | 0.493 | 0.456 | True Positive | Size Exclusion | Benign |
| $\begin{gathered} \hline 17 q 21.31 \\ \text { q21.32 } \end{gathered}$ | 124 | 139 | -0.856 | -1.015 | True Positive | Size Exclusion | Benign |
| 17q21.32 | 129 | 131 | -0.672 | -1.018 | True Positive | Size Exclusion | Benign |
| 19p13.3 | 216 | NA | -0.322 | NA | False Positive | Size Exclusion | Benign |
| 22q11.21 | 237 | 187 | -0.397 | -0.462 | True Positive | Size Exclusion | Benign |
| 22q11.21 | 190 | 239 | -0.419 | -0.387 | True Positive | Size Exclusion | Benign |
| $\begin{gathered} \text { Xq21.1q } \\ 28 \end{gathered}$ | 70741 | 70690 | -0.721 | -0.864 | True Positive | True Positive | Abnormal |

Note: Total True Negatives ( $>400 \mathrm{~Kb}$ analysis) $=29$. Values in brackets indicate an absence of a Nexus Copy Number CNV call but a CNV could be inferred through visual analysis of the region in question. The abnormality that was present in this array was the
Xq21.1q28 deletion of approximately 70 Mb in size. NA $=$ Not Applicable due to Size
Exclusion or inability to make a CNV call either by Nexus Copy Number or visual inspection. VUCS = Variant of Unclear Clinical Significance.

### 4.2 Significant CNV Metrics

In the 385 K CNV set, for 20 samples there were a total of 45 CNVs that were greater than 400 Kb and a total of 283 CNVs greater than 100 Kb (Shown in Table 4.2). In the 400 Kb CNV size cutoff analysis, CNVs with overlapping 720 K CNVs also had a higher $\log _{2}$ ratio than those that had no overlapping $720 \mathrm{~K} \mathrm{CNVs}$.In the 100 Kb CNV size cutoff analysis, CNVs with overlapping 720K CNVs had a higher mean $\log _{2}$ ratio value ( 0.542 vs. 0.506 ) and a higher median $\log _{2}$ value ( 0.477 vs. 0.452 ) than the 385 K CNVs with no overlapping 720K CNVs. An unpaired t-test was performed on the differing groups of $\log _{2}$ ratio means and found that the difference in $\log _{2}$ ratio means between the sets was statistically significantly different for the 400 Kb analysis ( $p=6.43 \times 10^{-11}$ ), but not significant for the 100 Kb analysis $(p=0.275)$. Subdividing these CNVs into deletions and duplications yielded statistically similar results for the 100 Kb . Statistical tests could not be performed for duplications and deletions separately in the 400 Kb CNV size cutoff group because of small numbers of CNVs. From these data we concluded the most appropriate threshold metric for future ROC analysis was the $\log _{2}$ ratio value and that our overall approach of using a higher resolution array to validate a lower resolution array was appropriate. The conclusions were based on the observation that CNVs with overlap (true positives) were represented by a significant amount of probes ( $p=0.0455$ ) that was greater than those CNVs without overlap (false positives). Thus, a CNV called with more probes had a higher probability of being confirmed with another array design

Table 4.2: Computer-aided single $\log _{2}$ ratio threshold comparison of two different array resolution designs.

| Type of CNV | Total Number of <br> All CNVs | Number of <br> Common CNVs | Number of <br> Unique CNVs |
| :--- | :---: | :---: | :---: |
| $>100 \mathrm{~Kb} 385 \mathrm{~K}$ CNVs with 720K Overlap | 211 | 107 | 104 |
| $>100 \mathrm{~Kb} 385 \mathrm{~K}$ CNVs without 720K Overlap | 72 | 32 | 40 |
| $>400 \mathrm{~Kb} 385 \mathrm{~K}$ CNVs with 720K Overlap | 43 | 24 | 19 |
| $>400 \mathrm{~Kb} 385 \mathrm{~K}$ CNVs without 720K Overlap | 2 | 0 | 2 |

### 4.3 ROC Analysis Results

Before performing the ROC analysis, the Nexus Copy Number ${ }^{\text {TM }}$ FASST algorithm was run with varying $\log _{2}$ ratio thresholds varying between 0.20 and 0.70 in increments of 0.05 to create 11 sets of CNV calls for both the 385 K and 720 K arrays. As described in the Approach section, a single $720 \mathrm{~K} \log _{2}$ threshold was used as a gold standard for each ROC analysis, while 385 K arrays for each $\log _{2}$ ratio threshold value were analyzed against it. This analysis was re-run for every $720 \mathrm{~K} \log _{2}$ ratio threshold value. There were 82 probes in the 385 K array that had poor coverage (no 720 K array probes within 15 Kb ) that were discarded from the experiment.

From the ROC curves an optimal value for the $\log _{2}$ ratio threshold was determined using normalized curves with a low FPR. The optimal $\log _{2}$ ratio thresholds for the 385 K array fell between 0.30 and 0.50 across all 720 K array $\log _{2}$ ratio threshold conditions. Optimal $\log _{2}$ ratio thresholds for deletions and duplications were similar but not exactly the same (Table 4.3).

Table 4.3: Optimal $\log _{2}$ ratio threshold determined for the 385 K array at every 720 K array $\log _{2}$ ratio threshold value including probes in common regions.

| 720K Gold Standard Log 2 Ratio | All CNV Types | Deletions | Duplications |
| :---: | :---: | :---: | :---: |
| 0.20 | 0.30 | 0.30 | 0.25 |
| 0.25 | 0.30 | 0.30 | 0.25 |
| 0.30 | 0.30 | 0.35 | 0.30 |
| 0.35 | 0.35 | 0.40 | 0.30 |
| 0.40 | 0.35 | 0.40 | 0.35 |
| 0.45 | 0.40 | 0.45 | 0.35 |
| 0.50 | 0.45 | 0.50 | 0.40 |
| 0.55 | 0.50 | 0.50 | 0.45 |
| 0.60 | 0.50 | 0.50 | 0.50 |
| 0.65 | 0.50 | 0.50 | 0.65 |
| 0.70 | 0.50 | 0.50 | 0.65 |

Note: The optimal $\log _{2}$ ratio was determined for deletions, duplications, and a combination of both deletions and duplications. These optimal $\log _{2}$ ratios were calculated from analyses in which probes in common CNV regions were included. Overall, larger $\log _{2}$ ratio thresholds are more appropriate for duplications than for deletions. The larger range for duplications is due to smaller numbers of CNV duplications.

Once the performance metrics were accurately calculated, the most appropriate $\log _{2}$ ratio threshold for the 385 K array platform that would meet the ACMG's guidelines of $>99 \%$ sensitivity and $<1 \%$ FPR was determined. While performing this analysis two cases were looked at, one with all CNVs taken together as well as one where CNVs that were be presumed to have clinical significance in constitutional/congenital genetic disorders. If all CNVs are included in the analysis the ACMG's guidelines with the 385 K array can not be met. However, when only those probes from CNVs that are considered clinically significant are included, it was determined that the best $\log _{2}$ ratio threshold to call duplications is 0.35 , which produces a sensitivity of $99.7 \%$ with a lower limit of the $95 \%$ confidence interval of $99.2 \%$ and a specificity of $99.9 \%$ (false positive rate of $0.06 \%$ with a higher limit at the $95 \%$ confidence interval of $0.08 \%$ ). Furthermore, it was
determined that the best $\log _{2}$ ratio threshold to call deletions is 0.40 , which produces a sensitivity of $99.8 \%$ with a lower limit at the $95 \%$ confidence interval of $99.3 \%$ and a specificity of nearly $100 \%$ ( $99.97 \%$ specificity with a false positive rate of $0.03 \%$ with a higher limit at the $95 \%$ confidence interval of $0.05 \%$ ). These performance metrics exceed those recommended by the ACMG. Table 4.4 shows optimal $\log _{2}$ ratios determined for analyses performed that excluded probes from common CNV regions.

Table 4.4: Optimal $\log _{2}$ ratio threshold determined for the 385 K array at every 720 K array $\log _{2}$ ratio threshold value excluding probes in common regions.

| 720K Gold Standard Log 2 Ratio | All CNV Types | Deletions | Duplications |
| :---: | :---: | :---: | :---: |
| 0.20 | 0.30 | 0.30 | 0.25 |
| 0.25 | 0.30 | 0.40 | 0.25 |
| 0.30 | 0.30 | 0.40 | 0.30 |
| 0.35 | 0.35 | 0.40 | 0.35 |
| 0.40 | 0.35 | 0.40 | 0.35 |
| 0.45 | 0.40 | 0.45 | 0.35 |
| 0.50 | 0.50 | 0.45 | 0.40 |
| 0.55 | 0.50 | 0.45 | 0.50 |
| 0.60 | 0.50 | 0.45 | 0.50 |
| 0.65 | 0.50 | 0.45 | 0.50 |
| 0.70 | 0.50 | 0.50 | 0.50 |

Note: These optimal $\log _{2}$ ratios were calculated from analyses in which probes in common CNV regions were excluded.

In addition to the comparison of the 385 K arrays to the 720 K arrays using 100 Kb and 400 Kb CNV size cutoffs, an analysis was performed comparing the 385 K arrays to the 2.1 M arrays using a 400 Kb CNV size cutoff. None of the 385 K array data used in the experiment corresponded to the data used in the 385 K array versus 720 K array experiment. In this analysis, there were 91 probes in the 385 K array that had poor coverage (no 2.1 M array probes within 15 Kb ) that were discarded from the experiment.

The results of this analysis did not perform as well as the comparison of the 385 K arrays to the 720 K arrays in analysis both including and excluding common CNV probes. This was due to the conditions in which the replicate arrays were created.

A sample of figures and tables for these analyses is shown in Appendix A. Due to the large number of figures for the analyses (66 in all) only a subset of the figures are shown for a single $\log _{2}$ ratio gold standard of 0.40 . Analysis for deletions, duplications, and a combination of both are shown on separate figures, while analyses including and excluding probes in common CNV regions are shown on the same figure.

## CHAPTER 5

## CONCLUSIONS

In this thesis it has been shown that clinical laboratories with access to two different resolution chromosomal microarray designs can perform a cost-effective analytical validation and calibration to establish the performance characteristics of their particular platform in their laboratory setting. Whereas we chose to perform this validation on NimbleGen whole-genome tiled CGH arrays, the methodology used is robust and should be applicable to other oligonucleotide-based designs.

The analytical procedure has been written so that it can be utilized on a typical desktop PC. When comparing 720 K arrays and 385 K arrays, the procedure uses approximately 2 GB of memory and takes approximately 2 hours to complete using a 2.5 GHz Core 2 Duo processor. The run time and memory usage of the procedure is highly dependent on the resolution of the microarray data and the algorithm parameters used to call CNVs and may increase greatly with the use of higher resolution chromosomal microarrays and lower algorithm thresholds resulting in more CNV calls.

Several technical problems are present when trying to perform an analytical validation of either the CMA technology or a specific platform. To validate the technology, a different test methodology should be used to confirm or refute the finding of the microarray, ideally at a resolution at which CMA possesses its greatest utility. Readily available technologies include FISH, quantitative PCR (qPCR), and multiplex ligation-dependent probe amplification (MLPA). The shortcoming of these approaches is that none of them is a genome wide screen. Comparison of microarray CNV findings with these technologies provides for identification of true and false positives but is generally lacking in true and false negatives. Without the later values, sensitivity and
specificity cannot strictly be calculated. These values could be calculated, for a limited, specific set of genetic loci but this is not an economical way to assess the genome-wide coverage of CMA. Conventional chromosome analysis (karyotyping) interrogates the entire genome, and as a comparison technology could be used to validate a whole genome chromosomal microarray. However, the resolution of chromosome analysis is such that only lesions of $>5 \mathrm{Mb}$ can be consistently and reliably validated. The method described here allows for calculation of true and false positives (as is done in most FISH, qPCR, or MLPA validations), as well as true and false negatives across the entire genome.

Previous publications have sought to prove the efficacy of chromosomal microarrays and provide a road map for clinical validation (Shaffer, et al. 2007; Shen and Wu, 2009; Yu, et al. 2009). Whereas each of these publications illustrates the importance of validation none provide a demonstrable method for the calculation of true and false negative values from CMA data. As both sensitivity and false positive rates rely on the ability to calculate true and false positives, as well as true and false negatives, these two additional metrics are necessary to adhere to the ACMG's guidelines.

This method is not without limitations. The gold standard used for the validation is another CMA design. The analysis of probe numbers in true and false positive CNVs suggests that this comparison is valid, yet does not address what is the most appropriate $\log _{2}$ ratio value to use with the higher resolution array. To compensate for this, the 385 K array was tested against higher resolution arrays at various $\log _{2}$ ratio thresholds and calculated the most appropriate $\log _{2}$ ratio threshold to use for the 385 K array at every higher resolution array $\log _{2}$ ratio threshold. This provided us with a range for the optimum $\log _{2}$ ratio threshold for the 385 K array design. This range, which was different for duplications and deletions (duplication range: $0.25-0.65$, deletion range: $0.30-$ 0.50 ), allowed us to determine what the optimal $\log _{2}$ ratio threshold should be when using
the 385 K array design to achieve the ACMG's recommendations for both sensitivity and specificity for simultaneous testing for both deletions and duplications.

We initially thought that the false positive rate might be better represented if the ROC analysis were performed for regions instead of probes, however conducting regionbased analyses proved challenging due to the incomplete classification of non-CNV regions with a truth-value. The arrays could be quantified into CNV regions and nonCNV regions, but precise classification of the regions proved difficult. We found that a probe-based analysis provided roughly uniform spacing and coverage between differing array types making it easier to assign truth-values to the probes.

Our validation design also has a very important difference from that suggested by the ACMG: the ability to include common, polymorphic CNVs. By including both unique and common CNVs we greatly increase the total number of CNV-related probes available for evaluation. An additional advantage of this approach is that following this type of validation the microarray platform under consideration has been appropriately calibrated to detect a wide range of polymorphic CNVs in addition to those that are currently sought after in constitutional genetic conditions. Whereas polymorphic CNVs are generally not considered significant in terms of developmental disorders, they have been shown in several publications to convey quantifiable risk of common diseases (Craddock, et al. 2010; Gamazon, Nicolae and Cox 2011). We observed that the sensitivity of our array platform is lower when considering all CNVs than when considering just those that are unique and likely clinically significant. We believe the explanation for this is that most common CNVs are part of segmental duplications and are very polymorphic in the general population. This makes the choice of reference DNA very important. We chose to use reference DNA that is a combination of genomic DNA from several individuals of the same sex. It is likely that within this mix of individuals there are different genotypes at several segmental duplication loci. This results in
"blunted" $\log _{2}$ ratio values of patient to reference signal at probes representing these loci. These lower ratios are often right at the $\log _{2}$ ratio threshold and are occasionally not detected on one or the other platform. Given that we are dealing with higher and lower resolution platforms, it is more common for these instances to be missed on the lower resolution platform and be classified as false negatives, thus lowering the sensitivity. All the false negatives we identified were within highly polymorphic regions of the genome and considered to be clinically benign.

As of the date of writing this thesis, only one major chromosomal microarray manufacturer (Affymetrix) has provided a statement that they have performed an analytical validation that meets or exceeds the ACMG recommendations. For clinical laboratories using microarrays from manufacturers that have yet to comply with the ACMG recommendations, as well as for laboratories to perform their own internal validation, our approach provides an alternative method to produce the same quality control and performance metrics required of any CLIA-certified laboratory.

## Future Work

Since the algorithm analyzes the data on a probe-by-probe basis it can be further optimized by examining the data on a CNV region based approach. A CNV region type approach could compare the CNV regions as they pertain to probes on the microarray. The amount probe overlap of lower resolution array CNVs by higher resolution array CNVs could be quantified to true positives, while the rest of the probes for the lower resolution array CNVs would be deemed false positives. The higher resolution array CNVs could be checked for overlapping lower resolution array CNVs. The false negatives could be quantified as the number of probes in the higher resolution array CNVs minus the amount of overlap that the higher resolution array CNVs had with the
lower resolution array CNVs. Finally the true negatives would be quantified as the total number of probes for all arrays minus the first three metrics calculated TP, FP, and FN. This is shown in equation 5.1.

Equation 5.1: Equation showing the sum of all binary classifier outcomes.
Total $=$ True Positives + False Positives + True Negatives + False Positives

This type of approach would greatly reduce the system memory usage as well as improve the total run time. Since computations performed could be exponentially reduced, it is possible that with this approach the run time could be reduced to minutes rather than hours.

## REFERENCES

Balif, B C, et al. "The clinical utility of enhanced subtelomeric coverage in array CGH." Am J Med Genet 143A, no. 16 (August 2007): 1850-7.

Beissbarth, Tim, Markus Ruschhaupt, David Jackson, Chris Lawerenz, and Ulrich Mansmann. "Recommendations for normalization of microarray data." 2005, 4.

BioDiscovery. "Nexus Copy Number User Manual Version 6." 2011.

Chen, Jeff. http://nim.vbi.vt.edu/~jeff/ImmArray/ (accessed June 2012).

Conrad, D F, D Pinto, R Redon, and et al. "Origins and functional impact of copy number variation in the human genome." Nature 464, no. 7289 (Apr 2010): 704-712.

Coulter, M E, D T Miller, D J Harris, and et al. "Chromosomal microarray testing influences medical management." Genet Med 13, no. 9 (Sep 2011): 770-776.

Craddock, N, M E Hurles, N Cardin, and et al. "Genome-wide association study of CNVs in 16,000 cases of eight common diseases and 3,000 shared controls." Nature 464, no. 7289 (Apr 2010): 713-720.
de Vet, Henrica C. W., et al. "Minimally important change determined by a visual method integrating an anchor-based and a distribution-based approach." Quality of Life Research 16 (2007): 131-142.

Gamazon, E R, D L Nicolae, and N J Cox. "A study of CNVs as trait-associated polymorphisms and as expression quantitative trait loci." PLoS Genet 7, no. 2 (2011): e1001292.

Hochstenback, R, E van Binsbergen, J Engelen, and et al. "Array analysis and karyotyping: workflow consequences based on a retrospective study of 36,325 patients with idiopathic developmental delay in the Netherlands." Eur J Med Genet 52, no. 4 (JulAug 2009): 161-169.

Kearney, H M, E C Thorland, K K Brown, F Quintero-Rivera, and S T South. "American College of Medical Genetics recommendations for the design and performance expectations for clinical genomic copy number microarrays intended for use in the postnatal setting for detection of constitutional abnormalities." Genet Med 13, no. 7 (July 2011): 680-685.

Kearney, H M, S T South, D J Wolff, A Lamb, A Hamosh, and K W Rao. "American College of Medical Genetics recommendations for the design and performance expectations for clinical genomic copy number microarrays intended for use in the postnatal setting for detection of constitutional abnormalities." Genet Med 13, no. 7 (July 2011): 676-679.

Krzanowski, Wojtek J, and David J Hand. ROC Curves for Continuous Datapublis. Boca Raton, Florida: CRC Press, 2009.

Manning, M, and L Hudgins. "Array-based technology and recommendations for utilization in medical genetics practice for detection of chromosomal abnormalities." Genet Med 12, no. 11 (Nov 2010): 742-745.

Marioni, J C, N P Thorne, and S Tavaré. "BioHMM: a heterogeneous hidden Markov model for segmenting array CGH data." Bioinformatics 22, no. 9 (May 2006): 1144-6.

McNamara, John. CPAN. Jan 3, 2011. http://search.cpan.org/~jmcnamara/Excel-Writer-XLSX-0.05/.

Miller, D T, M P Adam, S Aradhya, and et al. "Consensus statement: chromosomal microarray is a first-tier clinical diagnostic test for individuals with developmental disabilities or congenital anomalies." Am J Hum Genet 86, no. 5 (May 2010): 749-764.

Newcombe, R G. "Two-sided confidence intervals for the single proportion: comparison of seven methods." Stat Med 17, no. 8 (Apr 1998): 857-872.

O'Connor, Claire C. "Fluorescence In Situ Hybridization (FISH)." Nature Education 1, no. 1 (2008).

Pinto, Dalila, et al. "Comprehensive assessment of array-based platforms and calling algorithms for detection of copy number variants." Nature Biotechnology 29, no. 6 (June 2011): 512-520.

Quackenbush, J. "Microarray data normalization and transformation." Nature Genetics 32, no. 5 (Dec 2002): 496-501.

Roche NimbleGen. Human CGH Whole-Genome Tiling Arrays. Roche NimbleGen. http://www.nimblegen.com/products/cgh/wgt/human/index.html (accessed June 2012).

Shaffer, L G, A L Beaudet, A R Brothman, and et al. "Microarray analysis for constitutional cytogenetic abnormalities." Genet Med 9, no. 9 (Sep 2007): 654-662.

Shen, Y, and B L Wu. "Microarray-based genomic DNA profiling technologies in clinical molecular diagnostics." Clin Chem 55, no. 4 (Apr 2009): 659-669.

Shen, Y, K A Dies, I A Holm, and et al. "Clinical genetic testing for patients with autism spectrum disorders." Pediatrics 125, no. 4 (Apr 2010): e727-735.

Theisen, Aaron. "Microarray-based Comparative Genomic Hybridization (aCGH)." Nature Education 1, no. 1 (2008).

Venkatraman, E S, and Adam B Olshen. "faster circular binary segmentation algorithm for the analysis of array CGH data." Bioinformatics 23, no. 6 (March 2007): 657-663.

Vissers, L E, B B de Vries, and J A Veltman. "Genomic microarrays in mental retardation: from copy number variation to gene, from research to diagnosis." J Med Genet 47, no. 5 (May 2010): 289-297.

Yu, S, D C Bittel, N Kibiryeva, D L Zwick, and L D Cooley. "Validation of the Agilent 244K oligonucleotide array-based comparative genomic hybridization platform for clinical cytogenetic diagnosis." Am J Clin Pathol 132, no. 3 (Sep 2009): 349-360.

Zhang, Zhengdong D, and Mark B Gerstein. "Detection of copy number variation from array intensity and sequencing read depth using a stepwise Bayesian model." BMC Bioinformatics 11 (October 2010): 539.

Zou, Kelly H, James O'Mally, and Laura Mauri. "Statistical Primer for Cardiovascular Research." Circulation 115 (2007): 654-657.

## APPENDIX A

## COMPUTATIONAL ANALYSIS FIGURES AND TABLES

A. 1 Analysis of 385 K Versus 720 K (400Kb size cutoff)


Figure A.1: ROC plot of analysis comparing all 385 K CNVs (deletions and duplications) greater than 400 Kb to a 720 K gold standard $\log _{2}$ threshold of 0.40 . The solid line shows the analysis performed using all probes and the dotted line shows the analysis performed excluding probes from common CNV regions.

Table A.1: A table containing analysis results comparing all 385K CNVs (deletions and duplications) greater than 400 Kb to a 720 K gold standard $\log _{2}$ threshold of 0.40 . In this analysis, probes found in common CNV regions were included.

| 720K $\mathbf{L o g}_{2}$ Ratio | 385K Log 2 Ratio | FPR | Sensitivity | Normalized Optimal Distance |
| :---: | :---: | :---: | :---: | :---: |
| 0.40 | 0.20 | 0.035016867 | 0.998640196 | 1 |
| 0.40 | 0.25 | 0.016180212 | 0.998039216 | 0.462069491 |
| 0.40 | 0.30 | 0.007570203 | 0.984619935 | 0.216642703 |
| $\mathbf{0 . 4 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 0 0 2 8 6 6 9 5 5}$ | $\mathbf{0 . 9 5 6 3 5 7 9 2 8}$ | $\mathbf{0 . 0 9 2 1 7 3 4 2 8}$ |
| 0.40 | 0.40 | 0.002449858 | 0.931515536 | 0.097019123 |
| 0.40 | 0.45 | 0.001833528 | 0.765604681 | 0.239155274 |
| 0.40 | 0.50 | 0.001086957 | 0.647682119 | 0.352804159 |
| 0.40 | 0.55 | 0.000568692 | 0.530287648 | 0.469271392 |
| 0.40 | 0.60 | 0.00048891 | 0.449477352 | 0.550087834 |
| 0.40 | 0.65 | 0.000289412 | 0.39107703 | 0.608446594 |
| 0.40 | 0.70 | 0.000159692 | 0.179754373 | 0.820013545 |

Note: Numbers correspond to the data points shown in Figure A.1. The bolded row indicates the optimal $\log _{2}$ ratio found based on the closest linear distance (greyed box).

Table A.2: A table containing analysis results comparing all 385K CNVs (deletions and duplications) greater than 400 Kb to a 720 K gold standard $\log _{2}$ threshold of 0.40 . In this analysis, probes found in common CNV regions were excluded.

| 720K Log 2 Ratio | 385K Log 2 Ratio | FPR | Sensitivity | Normalized Optimal Distance |
| :---: | :---: | :---: | :---: | :---: |
| 0.40 | 0.20 | 0.016996157 | 1 | 1 |
| 0.40 | 0.25 | 0.007131854 | 0.999540863 | 0.419615948 |
| 0.40 | 0.30 | 0.002261443 | 0.998565966 | 0.133063859 |
| $\mathbf{0 . 4 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 0 0 0 3 8 2 6 4}$ | $\mathbf{0 . 9 9 6 5 1 0 4 6 9}$ | $\mathbf{0 . 0 2 2 7 8 2 1 6 8}$ |
| 0.40 | 0.40 | 0.000332306 | 0.979889392 | 0.028048372 |
| 0.40 | 0.45 | 0.000292038 | 0.792424242 | 0.208285711 |
| 0.40 | 0.50 | 0.000151076 | 0.691521961 | 0.308606078 |
| 0.40 | 0.55 | 0.000100721 | 0.633914422 | 0.366133541 |
| 0.40 | 0.60 | $2.01457 \mathrm{E}-05$ | 0.521857923 | 0.478143546 |
| 0.40 | 0.65 | $2.01457 \mathrm{E}-05$ | 0.477880939 | 0.522120406 |
| 0.40 | 0.70 | $2.01452 \mathrm{E}-05$ | 0.230585424 | 0.769415489 |

Note: Numbers correspond to the data points shown in Figure A.1. The bolded row indicates the optimal $\log _{2}$ ratio found based on the closest linear distance (greyed box).


Figure A.2: ROC plot of analysis comparing only 385 K CNV duplications greater than 400 Kb to a 720 K gold standard $\log _{2}$ threshold of 0.40 . The solid line shows the analysis performed using all probes and the dotted line shows the analysis performed excluding probes from common CNV regions.

Table A.3: A table containing analysis results comparing all 385K CNVs duplications greater than 400 Kb to a 720 K gold standard $\log _{2}$ threshold of 0.40 . In this analysis, probes found in common CNV regions were included.

| 720K Log 2 Ratio | 385K Log 2 Ratio | FPR | Sensitivity | Normalized Optimal Distance |
| :---: | :---: | :---: | :---: | :---: |
| 0.40 | 0.20 | 0.021158649 | 0.9986053 | 1 |
| 0.40 | 0.25 | 0.008268968 | 0.997037037 | 0.390811076 |
| 0.40 | 0.30 | 0.002998191 | 0.965546218 | 0.145516266 |
| $\mathbf{0 . 4 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 0 0 0 5 8 0 3 4 1}$ | $\mathbf{0 . 9 1 5 9 1 3 2 0 1}$ | $\mathbf{0 . 0 8 7 2 3 1 8 5 3}$ |
| 0.40 | 0.40 | 0.000507835 | 0.847272727 | 0.153432805 |
| 0.40 | 0.45 | 0.000487112 | 0.520183486 | 0.479642822 |
| 0.40 | 0.50 | 0.000466394 | 0.325966851 | 0.673938463 |
| 0.40 | 0.55 | 0.000228069 | 0.127071823 | 0.872817263 |
| 0.40 | 0.60 | 0.000228069 | 0.124309392 | 0.875583342 |
| 0.40 | 0.65 | 0.000124414 | 0.084714549 | 0.915186025 |
| 0.40 | 0.70 | 0 | 0 | 1 |

Note: Numbers correspond to the data points shown in Figure A.2. The bolded row indicates the optimal $\log _{2}$ ratio found based on the closest linear distance (greyed box).

Table A.4: A table containing analysis results comparing all 385 K duplications greater than 400 Kb to a 720 K gold standard $\log _{2}$ threshold of 0.40 . In this analysis, probes found in common CNV regions were excluded.

| 720K Log 2 Ratio | 385K Log $_{2}$ Ratio | FPR | Sensitivity | Normalized Optimal Distance |
| :---: | :---: | :---: | :---: | :---: |
| 0.40 | 0.20 | 0.011841112 | 1 | 1 |
| 0.40 | 0.25 | 0.004562548 | 0.998491704 | 0.385317064 |
| 0.40 | 0.30 | 0.001379339 | 0.994809689 | 0.116602876 |
| $\mathbf{0 . 4 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{4 . 1 8 5 3 3 E - 0 5}$ | $\mathbf{0 . 9 9 2 6 0 6 2 8 5}$ | $\mathbf{0 . 0 0 8 1 9 5 1 3 4}$ |
| 0.40 | 0.40 | $4.18533 \mathrm{E}-05$ | 0.931098696 | 0.068991904 |
| 0.40 | 0.45 | $2.09269 \mathrm{E}-05$ | 0.303030303 | 0.696971938 |
| 0.40 | 0.50 | $2.09269 \mathrm{E}-05$ | 0.015267176 | 0.98473441 |
| 0.40 | 0.55 | 0 | 0 | 1 |
| 0.40 | 0.60 | 0 | 0 | 1 |
| 0.40 | 0.65 | 0 | 0 | 1 |
| 0.40 | 0.70 | 0 | 0 | 1 |

Note: Numbers correspond to the data points shown in Figure A.2. The bolded row indicates the optimal $\log _{2}$ ratio found based on the closest linear distance (greyed box).


Figure A.3: ROC plot of analysis comparing all 385 K CNV deletions greater than 400 Kb to a 720 K gold standard $\log _{2}$ threshold of 0.40 . The solid line shows the analysis performed using all probes and the dotted line shows the analysis performed excluding probes from common CNV regions.

Table A.5: A table containing analysis results comparing all 385K CNVs deletions greater than 400 Kb to a 720 K gold standard $\log _{2}$ threshold of 0.40 . In this analysis, probes found in common CNV regions were included.

| 720K Log 2 Ratio | 385K Log ${ }_{2}$ Ratio | FPR | Sensitivity | Normalized Optimal Distance |
| :---: | :---: | :---: | :---: | :---: |
| 0.40 | 0.20 | 0.00610576 | 0.906613757 | 1 |
| 0.40 | 0.25 | 0.002425657 | 0.824661247 | 0.407427755 |
| 0.40 | 0.30 | 0.000940622 | 0.753401833 | 0.228673868 |
| 0.40 | 0.35 | 0.000539015 | 0.679071069 | 0.266053919 |
| 0.40 | 0.40 | 0.000566407 | 0.640112202 | 0.308242931 |
| 0.40 | 0.45 | 0.000383765 | 0.575357845 | 0.370743741 |
| 0.40 | 0.50 | 0.000347229 | 0.495769882 | 0.456717478 |
| 0.40 | 0.55 | 0.000319822 | 0.432797243 | 0.525240616 |
| 0.40 | 0.60 | 0.000246735 | 0.358446145 | 0.605980809 |
| 0.40 | 0.65 | 0.000155365 | 0.32008245 | 0.6474475 |
| 0.40 | 0.70 | 0.000146224 | 0.150280025 | 0.834583975 |

Note: Numbers correspond to the data points shown in Figure A.3. The bolded row indicates the optimal $\log _{2}$ ratio found based on the closest linear distance (greyed box).

Table A.6: A table containing analysis results comparing all 385 K deletions greater than 400 Kb to a 720 K gold standard $\log _{2}$ threshold of 0.40 . In this analysis, probes found in common CNV regions were excluded.

| 720K Log ${ }_{2}$ Ratio | 385K Log ${ }_{2}$ Ratio | FPR | Sensitivity | Normalized Optimal Distance |
| :---: | :---: | :---: | :---: | :---: |
| 0.40 | 0.20 | 0.005497415 | 1 | 1 |
| 0.40 | 0.25 | 0.002655081 | 1 | 0.482968973 |
| 0.40 | 0.30 | 0.000899455 | 1 | 0.163614086 |
| 0.40 | 0.35 | 0.000329017 | 0.997952218 | 0.059884498 |
| 0.40 | 0.40 | 0.000280643 | 0.997933884 | 0.051091851 |
| 0.40 | 0.45 | 0.000261294 | 0.970385675 | 0.056001216 |
| 0.40 | 0.50 | 0.000125825 | 0.938633194 | 0.065496167 |
| 0.40 | 0.55 | $9.67904 \mathrm{E}-05$ | 0.876552228 | 0.124697003 |
| 0.40 | 0.60 | $1.93594 \mathrm{E}-05$ | 0.731240429 | 0.268782642 |
| 0.40 | 0.65 | $1.93594 \mathrm{E}-05$ | 0.669472073 | 0.330546686 |
| 0.40 | 0.70 | $1.9359 \mathrm{E}-05$ | 0.335652174 | 0.664357159 |

Note: Numbers correspond to the data points shown in Figure A.3. The bolded row indicates the optimal $\log _{2}$ ratio found based on the closest linear distance (greyed box).


Figure A.4: ROC plot of analysis comparing all 385 K CNVs (deletions and duplications) greater than 100 Kb to a 720 K gold standard $\log _{2}$ threshold of 0.40 . The solid line shows the analysis performed using all probes and the dotted line shows the analysis performed excluding probes from common CNV regions.

Table A.7: A table containing analysis results comparing all 385K CNVs (deletions and duplications) greater than 100 Kb to a 720 K gold standard $\log _{2}$ threshold of 0.40 . In this analysis, probes found in common CNV regions were included.

| 720K $\mathbf{L o g}_{2}$ Ratio | 385K Log 2 Ratio | FPR | Sensitivity | Normalized Optimal Distance |
| :---: | :---: | :---: | :---: | :---: |
| 0.40 | 0.20 | 0.001570593 | 0.978944247 | 1 |
| 0.40 | 0.25 | 0.000830048 | 0.956085132 | 0.529008939 |
| 0.40 | 0.30 | 0.000472095 | 0.915377475 | 0.307517581 |
| $\mathbf{0 . 4 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 0 0 0 2 3 8 8 3 1}$ | $\mathbf{0 . 8 5 0 1 9 1 4 4 9}$ | $\mathbf{0 . 2 0 1 0 5 1 0 1 3}$ |
| 0.40 | 0.40 | 0.000143086 | 0.759376037 | 0.242087164 |
| 0.40 | 0.45 | $8.44499 \mathrm{E}-05$ | 0.633854955 | 0.356588895 |
| 0.40 | 0.50 | $5.42238 \mathrm{E}-05$ | 0.465916837 | 0.525197905 |
| 0.40 | 0.55 | $3.78786 \mathrm{E}-05$ | 0.390423889 | 0.60166219 |
| 0.40 | 0.60 | $2.99655 \mathrm{E}-05$ | 0.316125691 | 0.677343636 |
| 0.40 | 0.65 | $2.11444 \mathrm{E}-05$ | 0.275038921 | 0.719171388 |
| 0.40 | 0.70 | $1.73824 \mathrm{E}-05$ | 0.149188623 | 0.847674786 |

Note: Numbers correspond to the data points shown in Figure A.4. The bolded row indicates the optimal $\log _{2}$ ratio found based on the closest linear distance (greyed box).

Table A.8: A table containing analysis results comparing all 385 K CNVs (deletions and duplications) greater than 100 Kb to a 720 K gold standard $\log _{2}$ threshold of 0.40 . In this analysis, probes found in common CNV regions were excluded.

| 720K Log $_{2}$ Ratio | 385K $\mathbf{L o g}_{2}$ Ratio | FPR | Sensitivity | Normalized Optimal Distance |
| :---: | :---: | :---: | :---: | :---: |
| 0.40 | 0.20 | 0.000714305 | 0.993914807 | 0.455056827 |
| 0.40 | 0.25 | 0.000340923 | 0.982753581 | 0.21710135 |
| 0.40 | 0.30 | 0.000176022 | 0.969832736 | 0.112459378 |
| $\mathbf{0 . 4 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{5 . 7 4 5 2 1 E - 0 5}$ | $\mathbf{0 . 9 4 6 5 5 3 2 9 5}$ | $\mathbf{0 . 0 4 9 3 2 4 2 2 6}$ |
| 0.40 | 0.40 | $3.42876 \mathrm{E}-05$ | 0.893316599 | 0.090152559 |
| 0.40 | 0.45 | $2.01536 \mathrm{E}-05$ | 0.745210728 | 0.239105373 |
| 0.40 | 0.50 | $1.00768 \mathrm{E}-05$ | 0.542071197 | 0.446315709 |
| 0.40 | 0.55 | $6.93593 \mathrm{E}-06$ | 0.462540717 | 0.527529149 |
| 0.40 | 0.60 | $2.48646 \mathrm{E}-06$ | 0.387647832 | 0.604016468 |
| 0.40 | 0.65 | $1.17779 \mathrm{E}-06$ | 0.34376029 | 0.648846329 |
| 0.40 | 0.70 | $9.16056 \mathrm{E}-07$ | 0.171859296 | 0.824444451 |

Note: Numbers correspond to the data points shown in Figure A.4. The bolded row indicates the optimal $\log _{2}$ ratio found based on the closest linear distance (greyed box).


Figure A.5: ROC plot of analysis comparing only 385 K CNV duplications greater than 100 Kb to a 720 K gold standard $\log _{2}$ threshold of 0.40 . The solid line shows the analysis performed using all probes and the dotted line shows the analysis performed excluding probes from common CNV regions.

Table A.9: A table containing analysis results comparing all 385 K CNVs duplications greater than 100 Kb to a 720 K gold standard $\log _{2}$ threshold of 0.40 . In this analysis, probes found in common CNV regions were included.

| 720K Log 2 Ratio | 385K Log 2 Ratio | FPR | Sensitivity | Normalized Optimal Distance |
| :---: | :---: | :---: | :---: | :---: |
| 0.40 | 0.20 | 0.000760659 | 0.985650837 | 1 |
| 0.40 | 0.25 | 0.000333386 | 0.966031196 | 0.438737832 |
| 0.40 | 0.30 | 0.00017674 | 0.911764706 | 0.244144646 |
| $\mathbf{0 . 4 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{8 . 7 1 3 7 3 E - 0 5}$ | $\mathbf{0 . 8 1 3 1 2 5 6 9 5}$ | $\mathbf{0 . 2 0 9 1 9 0 6 6 1}$ |
| 0.40 | 0.40 | $4.82358 \mathrm{E}-05$ | 0.680457053 | 0.316063565 |
| 0.40 | 0.45 | $1.91904 \mathrm{E}-05$ | 0.471463023 | 0.522283079 |
| 0.40 | 0.50 | $1.41334 \mathrm{E}-05$ | 0.20261973 | 0.794647775 |
| 0.40 | 0.55 | $7.39086 \mathrm{E}-06$ | 0.135858378 | 0.862218537 |
| 0.40 | 0.60 | $6.09421 \mathrm{E}-06$ | 0.081270627 | 0.917581208 |
| 0.40 | 0.65 | $2.59328 \mathrm{E}-06$ | 0.066006601 | 0.9330387 |
| 0.40 | 0.70 | $7.77984 \mathrm{E}-07$ | 0.027640264 | 0.971957886 |

Note: Numbers correspond to the data points shown in Figure A.5. The bolded row indicates the optimal $\log _{2}$ ratio found based on the closest linear distance (greyed box).

Table A.10: A table containing analysis results comparing all 385 K duplications greater than 100 Kb to a 720 K gold standard $\log _{2}$ threshold of 0.40 . In this analysis, probes found in common CNV regions were excluded.

| 720K Log 2 Ratio | 385K Log | Ratio | FPR | Sensitivity |
| :---: | :---: | :---: | :---: | :---: | Normalized Optimal Distance

Note: Numbers correspond to the data points shown in Figure A.5. The bolded row indicates the optimal $\log _{2}$ ratio found based on the closest linear distance (greyed box).


Figure A.6: ROC plot of analysis comparing all 385 K CNV deletions greater than 100 Kb to a 720 K gold standard $\log _{2}$ threshold of 0.40 . The solid line shows the analysis performed using all probes and the dotted line shows the analysis performed excluding probes from common CNV regions.

Table A.11: A table containing analysis results comparing all 385 K CNVs deletions greater than 100 Kb to a 720 K gold standard $\log _{2}$ threshold of 0.40 . In this analysis, probes found in common CNV regions were included.

| 720K Log 2 Ratio | 385K Log ${ }_{2}$ Ratio | FPR | Sensitivity | Normalized Optimal Distance |
| :---: | :---: | :---: | :---: | :---: |
| 0.40 | 0.20 | 0.00080925 | 0.973801415 | 1 |
| 0.40 | 0.25 | 0.000496312 | 0.948508054 | 0.613848659 |
| 0.40 | 0.30 | 0.000295163 | 0.918117519 | 0.369192091 |
| 0.40 | 0.35 | 0.0001516 | 0.878185382 | 0.211506284 |
| 0.40 | 0.40 | 9.47975E-05 | 0.816800459 | 0.199288215 |
| 0.40 | 0.45 | $6.52298 \mathrm{E}-05$ | 0.750795948 | 0.24277669 |
| 0.40 | 0.50 | $4.00714 \mathrm{E}-05$ | 0.653722628 | 0.332398888 |
| 0.40 | 0.55 | $3.04749 \mathrm{E}-05$ | 0.572395527 | 0.413921692 |
| 0.40 | 0.60 | $2.38611 \mathrm{E}-05$ | 0.485154394 | 0.502658834 |
| 0.40 | 0.65 | $1.85442 \mathrm{E}-05$ | 0.425975573 | 0.563030747 |
| 0.40 | 0.70 | 1.65989E-05 | 0.238282431 | 0.755585415 |

Note: Numbers correspond to the data points shown in Figure A.6. The bolded row indicates the optimal $\log _{2}$ ratio found based on the closest linear distance (greyed box).

Table A.12: A table containing analysis results comparing all 385 K deletions greater than 100 Kb to a 720 K gold standard $\log _{2}$ threshold of 0.40 . In this analysis, probes found in common CNV regions were excluded.

| 720K Log 2 Ratio | 385K Log $\mathbf{2}^{2}$ Ratio | FPR | Sensitivity | Normalized Optimal Distance |
| :---: | :---: | :---: | :---: | :---: |
| 0.40 | 0.20 | 0.000337325 | 0.991845056 | 0.417248357 |
| 0.40 | 0.25 | 0.000191561 | 0.988769781 | 0.237212556 |
| 0.40 | 0.30 | $9.98363 \mathrm{E}-05$ | 0.975077882 | 0.123375828 |
| 0.40 | 0.35 | $3.49361 \mathrm{E}-05$ | 0.966004184 | 0.043907198 |
| $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 0}$ | $\mathbf{2 . 1 4 5 8 8 E - 0 5}$ | $\mathbf{0 . 9 5 1 9 2 8 1 5 6}$ | $\mathbf{0 . 0 3 4 7 5 1 6 3 1}$ |
| 0.40 | 0.45 | $1.47856 \mathrm{E}-05$ | 0.915605096 | 0.062492543 |
| 0.40 | 0.50 | $8.505 \mathrm{E}-06$ | 0.859275053 | 0.118076167 |
| 0.40 | 0.55 | $6.80399 \mathrm{E}-06$ | 0.756045137 | 0.223772673 |
| 0.40 | 0.60 | $2.48606 \mathrm{E}-06$ | 0.64235166 | 0.340380749 |
| 0.40 | 0.65 | $1.17761 \mathrm{E}-06$ | 0.570491803 | 0.414162574 |
| 0.40 | 0.70 | $9.15911 \mathrm{E}-07$ | 0.288526434 | 0.703712129 |

Note: Numbers correspond to the data points shown in Figure A.6. The bolded row indicates the optimal $\log _{2}$ ratio found based on the closest linear distance (greyed box).


Figure A.7: ROC plot of analysis comparing all 385 K CNVs (deletions and duplications) greater than 400 Kb to a 2.1 M gold standard $\log _{2}$ threshold of 0.40 . The solid line shows the analysis performed using all probes and the dotted line shows the analysis performed excluding probes from common CNV regions.

Table A.13: A table containing analysis results comparing all 385 K CNVs (deletions and duplications), greater than 400 Kb to a 720 K gold standard $\log _{2}$ threshold of 0.40 . In this analysis, probes found in common CNV regions were included.

| 2.1M Log 2 Ratio | 385K Log 2 Ratio | FPR | Sensitivity | Normalized Optimal Distance |
| :---: | :---: | :---: | :---: | :---: |
| 0.40 | 0.20 | 0.066232877 | 0.980582524 | 1 |
| 0.40 | 0.25 | 0.030079197 | 0.97810219 | 0.454150038 |
| $\mathbf{0 . 4 0}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 0 1 2 6 9 5 7 7 2}$ | $\mathbf{0 . 8 9 0 7 3 0 5 1}$ | $\mathbf{0 . 2 1 2 4 5 9 3 6 1}$ |
| 0.40 | 0.35 | 0.005159974 | 0.767844268 | 0.230514899 |
| 0.40 | 0.40 | 0.001608963 | 0.609715243 | 0.37899054 |
| 0.40 | 0.45 | 0.000512486 | 0.522790698 | 0.466921128 |
| 0.40 | 0.50 | 0.000153799 | 0.458891013 | 0.532027103 |
| 0.40 | 0.55 | 0.000146476 | 0.329174664 | 0.664310707 |
| 0.40 | 0.60 | $5.85956 \mathrm{E}-05$ | 0.256689792 | 0.738227772 |
| 0.40 | 0.65 | $3.66228 \mathrm{E}-05$ | 0.159585492 | 0.837254582 |
| 0.40 | 0.70 | 0 | 0.048245614 | 0.950799027 |

Note: Numbers correspond to the data points shown in Figure A.7. The bolded row indicates the optimal $\log _{2}$ ratio found based on the closest linear distance (greyed box).

Table A.14: A table containing analysis results comparing all 385 K CNVs (deletions and duplications), greater than 400 Kb to a 720 K gold standard $\log _{2}$ threshold of 0.40 . In this analysis, probes found in common CNV regions were excluded.

| 2.1M Log 2 Ratio | 385K Log 2 Ratio | FPR | Sensitivity | Normalized Optimal Distance |
| :---: | :---: | :---: | :---: | :---: |
| 0.40 | 0.20 | 0.04483012 | 0.95359116 | 1 |
| 0.40 | 0.25 | 0.016972437 | 0.946496815 | 0.37866759 |
| $\mathbf{0 . 4 0}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 0 0 5 5 1 3 8 9 5}$ | $\mathbf{0 . 7 7 4 1 5 1 4 3 6}$ | $\mathbf{0 . 2 2 4 8 0 3 8 5 8}$ |
| 0.40 | 0.35 | 0.001431988 | 0.571428571 | 0.402032432 |
| 0.40 | 0.40 | 0.000495006 | 0.357963875 | 0.624712529 |
| 0.40 | 0.45 | 0.000110864 | 0.296610169 | 0.688959011 |
| 0.40 | 0.50 | 0.000110864 | 0.227118644 | 0.761832087 |
| 0.40 | 0.55 | 0.000103474 | 0.227118644 | 0.76183157 |
| 0.40 | 0.60 | $2.21746 \mathrm{E}-05$ | 0.181328546 | 0.809846809 |
| 0.40 | 0.65 | $2.21746 \mathrm{E}-05$ | 0 | 1.000000122 |
| 0.40 | 0.70 | 0 | 0 | 1 |

Note: Numbers correspond to the data points shown in Figure A.7. The bolded row indicates the optimal $\log _{2}$ ratio found based on the closest linear distance (greyed box).


Figure A.8: ROC plot of analysis comparing all 385 K CNV duplications greater than 400 Kb to a 2.1 M gold standard $\log _{2}$ threshold of 0.40 . The solid line shows the analysis performed using all probes and the dotted line shows the analysis performed excluding probes from common CNV regions.

Table A.15: A table containing analysis results comparing all 385 K CNVs duplications greater than 400 Kb to a 2.1 M gold standard $\log _{2}$ threshold of 0.40 . In this analysis, probes found in common CNV regions were included.

| 2.1M Log 2 Ratio | 385K Log 2 Ratio | FPR | Sensitivity | Normalized Optimal Distance |
| :---: | :---: | :---: | :---: | :---: |
| 0.40 | 0.20 | 0.042554762 | 1 | 1 |
| 0.40 | 0.25 | 0.018065492 | 1 | 0.424523401 |
| 0.40 | 0.30 | 0.007054415 | 1 | 0.165772641 |
| $\mathbf{0 . 4 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 0 0 2 6 5 6 0 3 4}$ | $\mathbf{0 . 8 8 9 2 0 4 5 4 5}$ | $\mathbf{0 . 1 2 7 1 6 6 0 4 1}$ |
| 0.40 | 0.40 | 0.000839894 | 0.809756098 | 0.191264956 |
| 0.40 | 0.45 | $5.7746 \mathrm{E}-05$ | 0.645454545 | 0.354548051 |
| 0.40 | 0.50 | 0 | 0.535714286 | 0.464285714 |
| 0.40 | 0.55 | 0 | 0.535714286 | 0.464285714 |
| 0.40 | 0.60 | 0 | 0.535714286 | 0.464285714 |
| 0.40 | 0.65 | 0 | 0.535714286 | 0.464285714 |
| 0.40 | 0.70 | 0 | 0 | 1 |

Note: Numbers correspond to the data points shown in Figure A.8. The bolded row indicates the optimal $\log _{2}$ ratio found based on the closest linear distance (greyed box).

Table A.16: A table containing analysis results comparing all 385 K duplications greater than 400 Kb to a 2.1 M gold standard $\log _{2}$ threshold of 0.40 . In this analysis, probes found in common CNV regions were excluded.

| 2.1M Log 2 Ratio | 385K Log 2 Ratio | FPR | Sensitivity | Normalized Optimal Distance |
| :---: | :---: | :---: | :---: | :---: |
| 0.40 | 0.20 | 0.027314036 | 1 | 1 |
| 0.40 | 0.25 | 0.009570851 | 1 | 0.35040048 |
| 0.40 | 0.30 | 0.003066613 | 1 | 0.112272435 |
| 0.40 | 0.35 | 0.00058246 | 1 | 0.021324574 |
| $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 0 0 0 2 9 1 3 1 3}$ | $\mathbf{1}$ | $\mathbf{0 . 0 1 0 6 6 5 3 2 4}$ |
| 0.40 | 0.45 | 0 | 0 | 1 |
| 0.40 | 0.50 | 0 | 0 | 1 |
| 0.40 | 0.55 | 0 | 0 | 1 |
| 0.40 | 0.60 | 0 | 0 | 1 |
| 0.40 | 0.65 | 0 | 0 | 1 |
| 0.40 | 0.70 | 0 | 0 | 1 |

Note: Numbers correspond to the data points shown in Figure A.8. The bolded row indicates the optimal $\log _{2}$ ratio found based on the closest linear distance (greyed box).


Figure A.9: ROC plot of analysis comparing all 385 K CNV deletions greater than 400 Kb to a 2.1 M gold standard $\log _{2}$ threshold of 0.40 . The solid line shows the analysis performed using all probes and the dotted line shows the analysis performed excluding probes from common CNV regions.

Table A.17: A table containing analysis results comparing all 385K CNVs deletions greater than 400 Kb to a 2.1 M gold standard $\log _{2}$ threshold of 0.40 . In this analysis, probes found in common CNV regions were included.

| 2.1M Log 2 Ratio | 385K Log 2 Ratio | FPR | Sensitivity | Normalized Optimal Distance |
| :---: | :---: | :---: | :---: | :---: |
| 0.40 | 0.20 | 0.021191012 | 0.971409122 | 1 |
| 0.40 | 0.25 | 0.010629848 | 0.968773234 | 0.501627918 |
| $\mathbf{0 . 4 0}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 0 0 5 0 7 3 9 9 6}$ | $\mathbf{0 . 8 4 6 4 1 9 3 2 7}$ | $\mathbf{0 . 2 7 1 8 2 2 6 5 6}$ |
| 0.40 | 0.35 | 0.002300511 | 0.726570048 | 0.274430763 |
| 0.40 | 0.40 | 0.000699889 | 0.568250758 | 0.416336368 |
| 0.40 | 0.45 | 0.000479801 | 0.50880829 | 0.47675422 |
| 0.40 | 0.50 | 0.000165228 | 0.452182952 | 0.534565096 |
| 0.40 | 0.55 | 0.000157361 | 0.311064718 | 0.679820467 |
| 0.40 | 0.60 | $6.295 \mathrm{E}-05$ | 0.231351351 | 0.76184522 |
| 0.40 | 0.65 | $3.93447 \mathrm{E}-05$ | 0.123723042 | 0.87263747 |
| 0.40 | 0.70 | 0 | 0.050400916 | 0.948115665 |

Note: Numbers correspond to the data points shown in Figure A.9. The bolded row indicates the optimal $\log _{2}$ ratio found based on the closest linear distance (greyed box).

Table A.18: A table containing analysis results comparing all 385 K deletions greater than 400 Kb to a 2.1 M gold standard $\log _{2}$ threshold of 0.40 . In this analysis, probes found in common CNV regions were excluded.

| 2.1M Log Ratio | 385K Log Ratio | FPR | Sensitivity | Normalized Optimal Distance |
| :---: | :---: | :---: | :---: | :---: |
| 0.40 | 0.20 | 0.015715403 | 0.943925234 | 1 |
| 0.40 | 0.25 | 0.006650783 | 0.941258741 | 0.42321097 |
| $\mathbf{0 . 4 0}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 0 0 2 1 7 9 1 8 4}$ | $\mathbf{0 . 7 5 5 3 0 4 1 0 2}$ | $\mathbf{0 . 2 4 3 2 2 5 6 0 5}$ |
| 0.40 | 0.35 | 0.000825213 | 0.559865093 | 0.410249965 |
| 0.40 | 0.40 | 0.000174677 | 0.340640809 | 0.639219746 |
| 0.40 | 0.45 | 0.000119104 | 0.296610169 | 0.685811302 |
| 0.40 | 0.50 | 0.000119104 | 0.227118644 | 0.759426977 |
| 0.40 | 0.55 | 0.000111165 | 0.227118644 | 0.759422104 |
| 0.40 | 0.60 | $2.38229 \mathrm{E}-05$ | 0.181328546 | 0.807900884 |
| 0.40 | 0.65 | $2.38228 \mathrm{E}-05$ | 0 | 1.000001149 |
| 0.40 | 0.70 | 0 | 0 | 1 |
| N |  |  |  |  |

Note: Numbers correspond to the data points shown in Figure A.9. The bolded row indicates the optimal $\log _{2}$ ratio found based on the closest linear distance (greyed box).

## APPENDIX B

## COMPUTATIONAL ANALYSIS CODE

## B. 1 Microarray Evaluation Script

```
#!/usr/bin/perl
# Written by Corey Goodman - Electrical and Computer Engineering, University of
Iowa
# Version 1.0
use strict;
use warnings;
use Getopt::Long qw(:config gnu__getopt);
use Scalar::Util qw(looks_like_number);
sub usage {
    print <<"USAGE";
Usage: perl $0 [OPTIONS] <input_directory> <output_directory>
<input_directory> Input directory containing CNV call files, microarray
    files, and a common location file if needed
<output_directory> Name of the output directory where the results of the
    analysis are placed. If specified directory does not
    exist the directory is created.
-s, --small Small resolution array unique identifier key used in
    CNV call files in first column (required)
-l, --large Large resolution array unique identifier key used in
    CNV call files in first column (required)
-q, --quiet Flag used to suppress output while analysis is running
                                If not specified script progress is printed while running
    (optional)
-b, --buffer Buffer used when calling CNVs (optional, default=15000)
-m, --minsize Minimum CNV size used for TP/FN (optional, default=400000)
-c, --common Exclude common CNV probes from analysis the average
    CNV size (optional)
-g, --gains Include CNV duplications in analysis.
    If neither -g or -d flag is set both CNV types are included
-d, --deletions Include CNV deletions in analysis.
        If neither -g or -d flag is set both CNV types are included
-h, --help Print this message
ARRAY IDS USED TO LABEL INDIVIDUAL CNV CALLS IN THE CNV CALL FILES AND USED TO
LABEL THE ARRAY FILE NAMES BE THE SAME. MAKE SURE THE -s AND -l ARGUMENTS MATCH
THESE IDENTIFIERS.
IF AN EXISTING FILE IS SPECIFIED AS OUTPUT IT WILL BE OVERWRITTEN
```

```
format of input_directory files
```

format of input_directory files
<cnv_call_files>
Required to begin with a log2 ratio threshold (number) used to call
CNVs
followed by an underscore
Example: 0.30_CNVCalls.txt

```
```

<common_file> (optional)
Required to be named: CommonLocations.txt
Note: Can not perform analysis excluding common probes if this file
does not exist.
<low_resolution_array>
Required to begin with the word "Array_" then a unique array type
identifier different from the higher resolution array then and
underscore and any desired text
Example: Array_385k_segMNT.txt
Note: The array is used for probe positions only so only information
in the array file related to probe positions is needed.
<high_resolution_array>
Required to begin with the word "Array_" then a unique array type
identifier different from the lower resolution array then and
underscore and any desired text
Example: Array_720k_segMNT.txt
Note: The array is used for probe positions only so only information
in the array file related to probe positions is needed.

```

Note: All files must end with a ".txt" extension and have UNIX line endings. The first line of all files is expected to be a header line and is not parsed out. The files are all tab delimitated with no quotation marks surrounding fields. On most unix platforms line endings can be converted with "dos2unix". Array type identifier for microarrays must be the same identifier specified in probe_roc.pl script
**When defining columns in files (below)
\(r c=\) required column column must be present and meet formatting standards set
uc = unimportant column column must be present but does not need to meet any format standards
nc \(=\) non-required column column does not need to be present
format of CNV call file names:
[log2 ratio]_[filename].txt e.g. 0.30_CNVCalls.txt
format of <CNV_call_file>:
(Column Fiē̆d Description [Field Format Descriptiion])
rc1: Sample name
Format: [patient unique id] [array type identifier]
rc2: Genomic position
Format: [chromosome]: [start]-[stop]
Note: chromosome is in the format chr[XX] where XX is chromosome identifier
rc3: CNV event
Possibilities: Gain, Loss
uc4: CNV length
uc5: Cytoband
uc6: Probe log2 median
rc7: Number of probes
Note: array type identifier in cl must be the same identifier specified in
probe_roc.pl script
The analysis types possible are:
Both - Analysis includes deletions and duplications
Gain - Analysis includes duplications only
Loss - Analysis includes deletions only
```

format of <microarray files>:
uc01: INDEX
uc02: X
uc03: Y
uc04: CONTAINER
uc05: SEQUENCE ID
uc06: PROBE_ID
rc07: POSITION
Note: this column is used by probe_roc.pl script
uc08: GC
rc09: CHROMOSOME
Format: chr[XX] where XX is chromosome identifier
Note: this column is used by probe_roc.pl script
nc10: CHR POSITION
nc11: EXP_405948_2011-08-15_Slot2_532
nc12: REF_405948_2011-08-15_Slot2_635
nc13: RATİO
nc14: EXP_SPATIAL
nc15: REF SPATIAL
nc16: RATIO_SPATIAL
nc17: EXP_NORM
nc18: REF NORM
nc20: RATİO_CORRECTED
format of ROC analysis output file names:
[log2 ratio]_[analysis type]_Results.txt e.g. 0.30_Both_Results.txt
format of output files:
(Only results files should be in the directories)
rc1: gold standard (higher resolution) log2 ratio
rc2: lower resolution log2 ratio
rc3: True Positives (TP)
rc4: False Positives (FP)
rc5: True Negatives (TN)
rc6: False Negatives (FN)
rc7: Discarded Probes
rc8: Total Probes
Notice: analysis including CNVs on the X/Y chromosome should be
interpreted with caution.
USAGE
exit;
}

```
my \$key_small = '';
my \$key_large = '';
my \$common_discard = '';
my \$quiet = '';
my \$distance buffer = 15000;
my \$size_cutoff = 400000;
my \$gain_included = '';
my \$loss_included = '';
my \$opt_ok = GetOptions (
        's|small=s' \(\quad>\quad\) \\$key small,
        'l|large=s' => \\$key_Iarge,
        'q|quiet' \(=>\) \\$quiet,
        'c|common' \(=>\) \\$common_discard,
        'b|buffer=i' => \\$distance_buffer,
        'm|minsize=i' => \\$size_cutoff,
```

        'g|gains' => \$gain included,
        'd|deletions' => \$loss_included,
        'h|help' => sub { usage(); },
    );
usage() unless ((@ARGV == 2) \&\& \$key_small \&\& \$key_large);
my \$input_dir = \$ARGV[0];
$input_dir .= '/' unless substr($input_dir,-1,1) eq '/';
my \$output_dir = \$ARGV[1];
$output_dir .= '/' unless substr($output_dir,-1,1) eq '/';

# check input and output directories

if (!(-d \$input_dir)) {
warn 'The iñput directory does not exist!'."\n\n";
usage();
}
if (!(-d \$output_dir)) {
warn 'The output directory does not exist, creating directory...'."\n";
if (!(mkdir $output_dir)) {
            warn 'Can not create directory: '.$output_dir."\n\n";
usage();
}
}
my \$postfix = \$common_discard ? '_NoCommon' : '_Results';

# default variables that can't be set in options

my \$common_file = "CommonLocations.txt";

# Hash Keys

my \$gain_key = "Gain";
my \$loss_key = "Loss";
my \$both_key = "Both";
my \$none_key = "None";
my \$chr_\overline{key = "chr";}
my \$start_key = "start";
my \$stop_key = "stop";
my \$call_type_key = "call type";
my \$large_key = "Large";

# determined by -g and -d flags

# set CNV types used for analysis

my \$type_key1 = \$gain_key;
my \$type_key2 = $loss_key;
if ($gain_included \&\& !\$loss_included) {
\$type_key2 = $gain_key;
}
elsif (!$gain_included \&\& \$loss_included) {
\$type_key1 = \$loss_key;
}
my $output_type = ($type_key1 eq \$type_key2) ? \$type_key1 : \$both_key;
my %common_cnvs = ();
my @log_ratios = ();
my %patient_ids = ();
my \$array_fīile_large = '';
my \$array_file_small = '';

```
```

my %cnv calls large = ();
my %cnv_calls_small = ();
print 'Reading input files...'."\n" unless \$quiet;
opendir(IN_DIR, $input_dir) or die 'Could not open input directory: '
    .$input_dir." : \$!\n";
my @input_files = readdir(IN_DIR);
foreach my $input_file (@input_files) {
    # ignore hidden files
    if(!($input_file =~ m/^(\.)/i)) {
\# Put Common CNV Calls into hash
if (\$input_file eq $common_file) {
            if($common_discard) {
open(IN, '< '.$input_dir.$common_file) or die
'Can\'t open common file-'.\$common_file." : \$!\n";
my \$line = <IN>; \#Remove the header
my $count = 0;
                # read common CNVs into hash
                while($line = <IN> ) {
chomp \$line;
my @line_data = split("\t", \$line);
\#turn liñe into an array of elements
\# fromat cnv location info
my \$loc = \$line_data[0];
\$loc =~ tr/,//d;
\$loc =~ tr/:/-/;
my @location_info = split("-", \$loc);
my \$chr = \$location_info[0];
my \$start = \$location_info[1];
my \$stop = \$location_info[2];
$common_cnvs {$chr}{\$start} = $stop;
                } # end looping through file
                close(IN);
            }
        }
            elsif ($input_file =~ m/^(Array)/i) {
my @file_parts = split('_', $input_file);
            if ($file_parts[1] eq \$key_small) {
\$array_file_small = $iñput_dir.$input_file;
}
elsif (\$file_parts[1] eq \$key_large) {
\$array_fīle_large = $input_dir.$input_file;
}
}
\# files should be cnv call files
else {
\# ensure file name is formatted correctly
my @file_parts = split('_', $input_file);
            if (looks_like_number($file_parts[0])) {
my \$lōg_ratio = \$file_parts[0];
\# add log-ratio to list
push(@log_ratios, $log_ratio);
                # Put cnv Calls into hash
                open(IN, '< '.$input_dir.$input_file) or die
                                    'Can\'t open CNV file '.$input_file." : \$!\n";
my \$line = <IN>; \#Remove the header

```
```

        # loop over each CNV call
        while($line = <IN> ) {
        chomp $line;
        my @line_data = split("\t", $line);
        #turn line into an array of elements
        # format patient info
        my @patient_info = split("_", $line_data[0]);
        my $array_type = $patient_info[1];
        my $patient = $patient_info[0];
        # push patient id onto hash
        $patient_ids{$patient} = 1;
        my @temp = split(" ", $line_data[2]);
        my $call_type = $temp[@temp-1];
        # fromat cnv location info
        my $loc = $line_data[1];
        $loc =~ tr/,//d;
        $loc =~ tr/:/-/;
        my @location_info = split("-", $loc);
        my $chr = $location_info[0];
        my $start = $locatiōn_info[1];
        my $stop = $location_info[2];
        # filter by designated call type
        if ($call_type eq $type_key1 || $call_type eq $type_key2) {
        #my $length = $stop - $start;
        # put CNV calls in appropriate hash
        if ($array_type eq $key_small) {
                $cnv_calls_small{$log_ratio} {$patient} {$chr}
                            {$start}{$chr_key} = $chr;
                $cnv_calls_small{$log_ratio}{$patient}{$chr}
                            {$start}{$start_key} = $start;
                $cnv_calls_small{$log_ratio} {$patient} {$chr}
                                    {$start}{$stop_key} = $stop;
                $cnv_calls_small{$log_ratio}{$patient}{$chr}
                    {$start}{$cal\overline{l_type_key} = $call_type;}
                }# end type check
                elsif ($array_type eq $key_large) {
                $cnv_call\overline{s_large{$log_ratio} {$patient}{$chr}}
                        {$start}{$chr_key} = $chr;
                $cnv_calls_large{$log_ratio} {$patient} {$chr}
                                    {$start}{$start_key} = $start;
                $cnv_calls_large{$log_ratio} {$patient} {$chr}
                        {$start}{$stop key} = $stop;
                $cnv_calls_large{$log_ratio} {$patient}{$chr}
                {$start}{$call_type_key} = $call_type;
        }# end type check
        }
    } \# end looping through file
close(IN);
}
else {
warn 'Improperly formatted files exist in input directory: '
.\$input_file."\n";
}
}

```
```

}
closedir(IN_DIR);
if (!$array_file_small || !$array_file_large) {
warn 'The microarray keys entered ['.$key_small.', '.$key_large.
'] could not be matched to corresponding microarray files'."\n";
usage();
}

# sort ratios in ascending order

@log_ratios = sort { \$a <=> $b } @log_ratios;
print "Analysis being performed for type: ".$output_type."\n" unless \$quiet;
my %probes_small = ();
my %probes_large = ();
my \$discarded = 0;
print 'Reading probes from large array file...'."\n" unless \$quiet;

# Open large microarray file

open(IN, '< '.$array_file_large) or die "Can't open ".$array_file_large.
" : \$!\n";
my $line = <IN>; #Remove the header
while($line = <IN> ) {
chomp \$line;
my @line_data = split("\t", \$line); \#turn line into an array of elements
my \$chr = \$line_data[0];
my \$pos = \$line_data[1];
my $common_overlap = '';
    if ($common_discard) {
foreach my $common_start (keys %{$common_cnvs{\$chr}}) {
my $common_sto\overline{p}=$common_cnvs{$chr}
            if ($pos >= \$common_start \&\& \$pos <= \$common_stop) {
$common_overlap = 1;
                last;
                    }
            }
        }
        if (!$common_overlap) {
push(@{$probes_large{$chr}}, \$pos);
}
}
close(IN);
print 'Reading probes from small array file...'."\n" unless \$quiet;

# open small microarray file

open(IN, '< '.$array_file_small) or die "Can't open ".$array_file_small.
" : \$!\n";
$line = <IN>;
while($line = <IN> ) {
chomp \$line;
my @line_data = split("\t", \$line); \#turn line into an array of elements
my \$chr = \$line_data[0];
my \$pos = \$line_data[1];
my $common_overlap = '';
    if ($common_discard) {
foreach my $common_start (keys %{$common_cnvs{\$chr}}) {
my $common_sto\overline{p}=$common_cnvs{$chr}{$common_start};
if (\$pos >= \$common_start \&\& \$pos <= \$common_stop) {

```
```

                $common overlap = 1;
                last;
                }
        }
    }
    if (!$common_overlap) {
        push(@{$probes_small{$chr}}, $pos);
    }
    else {
        $discarded++;
        }
    }
close(IN);

```
```

print 'Sorting probe arrays...'."\n" unless \$quiet;
\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#

# Sort arrays

foreach my $chr (keys %probes_small) {
    @{$probes_small{\$chr}} = Sort { \$a <=> $b } @{$probes_small{\$chr}};
}
foreach my $chr (keys %probes_large) {
    @{$probes_large{\$chr}} = 'sort { \$a <=> $b } @{$probes_large{\$chr}};
}

```
```

print 'Discarding poor coverage probes...'."\n" unless \$quiet;
\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#

# Find probes to throw out

my %throw_out;

# loop over each chromosome

foreach my \$chr (keys %probes_small) {
my \$lastIndex = 0;
my \$found;
my \$probe_pos;
my \$count = 0;
my @indices = ();
for(my \$i = 0; $i < @{$probes_small{\$chr}}; \$i++) {
my \$probe_pos = ${$probes_small{$chr}}[$i];
my \$index = \$lastIndex;
$found = 0;
        # loop until:
            end of large array probes is reached
            large array probe location has surpassed small array probe
            location + distance_buffer a corresponding probe is found
        while ($index < @{$probes_large{$chr}} \&\&
${$probes_large{$\overline{chr}}}[$index] < \$probe_pos + $distance_buffer
                        && !$found) {
\# check if large-array probe is within distance_buffer of
\# small-array probe
if (abs(\$probe_pos - ${$probes_large{$chr}}[$index]) <
\$distance_buffer) {
push(@indices, \$i);
\$discarded++;
\$found = 1;
}

```
```

                if (${$probes large{$chr}}[$index] < $probe pos) {
                $lastIndex = ${$probes_large{$chr}}[$in\overline{dex];}
            }
                $index++;
        }
    }
    foreach my $i (reverse(sort { $a <=> $b } @indices)) {
        splice(@{$probes small{$chr}}, $i, 1);
    }
    }
\$discarded *= keys(%patient_ids);
\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#

# Map large CNV calls to hash

foreach my \$ratio_large (@log_ratios) {
\#Building large to small maps
my %overlap = ();
foreach my $patient (keys %patient_ids) {
    my %cnv_map_large = ();
    print 'Building map for '.$ratio_large.', '.\$patient.'...'."\n"
unless \$quiet;
foreach my \$chr (keys %probes_large) {
for (my \$i = 0; $i < @{$probes_large{\$chr}}; \$i++) {
$cnv_map_large {$patient} {$\overline{chr } {${$probes_large {$chr} }[\$i]} = 0;}
}
my \$last_index = 0;
foreach my $position_large (sort {$a<=>$b} keys
                    %{$cnv calls-
my \$start = $cnv_calls_large{$ratio_large}{$patient}
                    {$chr} {$position_large} {$start_key};
my \$stop = $cnv_calls_la\overline{rge{$ratio_large}{$patient}}
                    {$chr} {$position_large}{$stop_key};
my $type = ($cnv_calls_large{$ratio_large}{$patient}
{$chr} {$\overline{positiōn_large}{\$ca\overline{l}_type_key} eq \$gain_key) ?}
1 : -1;
my \$index = $last_index;
                while ($index < @{$probes_large{$chr}} \&\&
${$probes_large{$chr}}[$index] < \$start) {
$index++;
                }
                while ($index < @{$probes_large{$chr}} \&\&
${$probes_large{$chr}}[$index] < $stop) {
                    if (${$probes_large{$chr}}[\$index] >= \$start \&\&
${$probes_large{$chr}} [$index] <= $stop) {
                if ($stop - \$start >= \$size_cutoff) {
$cnv_map_large{$patient}{$chr}
                                    {${$probes_large{$chr} }[\$index]} =
\$type * 2;
}
else {
$cnv_map_large{$patient}{$chr}
                                    {${$probes_large{$chr} } [\$index] } = \$type;
}
}
\$index++;
}

```
```

    $last_index = $index;
    }
    $last index = 0;
    for (my $i = 0; $i < @{$probes_small{$chr}}; $i++) {
        my $position_small = ${$probes_small{$chr}}[$i];
        my $index = $last index;
        $overlap{$patient} {$chr} {$position_small}{$gain_key} = 0;
        $overlap{$patient} {$chr} {$position_small}{$loss_key} = 0;
        $overlap{$patient} {$chr}{$position_small}{$none_key} = 0;
        while ($index < @{$probes_large{$chr}} &&
            ${$probes_large{$chr}}[$index] <
                ${$probes_small{$chr}}[$i]-$distance_buffer) {
            $index++;
        }
        $last_index = $index;
        while ($index < @{$probes_large{$chr}} &&
            ${$probes_large{$chr}}[$index] <
            ${$probes_small{$chr}}[$i]+$distance buffer) {
            if ($cnv_map_large{$patient}{$chr}
                    {${$\overline{probes_large{$chr}}[$index]} >= 1) {}
                $overlap{$pati\overline{ent}{$chr}{$position small}{$gain key}=1;}
                if ($cnv_map_large{$patient}{$chr}
                    {${$probes_large{$chr}}[$index]} == 2) {
                    $overlap{$pati\overline{ent} {$chr}}
                        {$position_small}{$large_key} = 1;
                }
            else {
                    $overlap{$patient} {$chr} {$position_small}
                                    {$large_key} = 0;
            }
            }
            elsif ($cnv map large{$patient}{$chr}
                    {${堷ro\overline{bes_large{$chr}}[$index]} <= -1) {}
                $overlap{$patient} {$chr} {$position_small}{$loss_key}=1;
                if ($cnv_map_large{$patient}{$chr}
                        {${$probes_large{$chr}}[$index]} == -2) {
                    $overlap{$pati\overline{ent} {$chr}}
                                    {$position_small}{$large_key} = 1;
            }
            else {
                    $overlap { $patient} { $chr}
                                    {$position_small}{$large_key} = 0;
            }
            }
            else {
                        $overlap {$patient} {$chr}
                            {$position_small}{$none_key} = 1;
            }
            $index++;
        }
    }
    %cnv_map_large = ();
    unde}\overline{f}%c\overline{n}v_map_large
    }
    }

# Done building large to small maps

# Region outfile

open(OUTFILE, ">".$output_dir.$ratio_large.'_'.

```
```

        $output type.$postfix.'.txt');
    print OUTFILE $key_large.' Ratio'."\t".$key_small.' Ratio'."\t".'TP'.
"\t".'FP'."\t".'TN'."\t".'FN'."\t".'Discarded'."\t".'Total'."\n";
close(OUTFILE);
foreach my $ratio small (@log ratios) {
    print 'Assignīng truth values '.$ratio_large.' <= '.
\$ratio_small.'...'."\n" unless \$quiet;
my \$TP = 0;
my \$FP = 0;
my \$TN = 0;
my \$FN = 0;
foreach my \$patient (keys %patient_ids) {
my %cnv_map_small = ();
foreach my \$chr (keys %probes_small) {
for (my \$i = 0; $i < @{$probes small{\$chr}}; \$i++) {
$cnv_map_small{$patient}{$chr}
                            {${$probes_small{$chr}}[\$i]} = 0;
}
my \$last index = 0;
foreach my $position_small (sort {$a<=>$b} keys
            %{$cnv_calls_small{$ratio_small}{$patient}{\$chr}}) {
my \$start = $cnv_calls_small{$ratio_small}{$patient}
                    {$chr}{$\overline{positiōn_small}{$stārt key};}
my \$stop = $cnv_calls_small{$ratio_small}{$patient}
                    {$chr}{$position small}{$stop key};
my $type = ($cnv_calls_small{$ratio_small}{$patient}
{$chr}{$position_small}{\$call_type_key} eq
\$gain key) ? 1 : -1;
my \$index = $last_index;
                while ($index < @{$probes_small{$chr}} \&\&
${$probes_small{$\overline{chr}}}[$index] < \$start) {
$index++;
            }
                while ($index < @{$probes_small{$chr}} \&\&
${$probes_small{$chr}}[$index] < $stop) {
        if (${$probes_small{$chr}}[\$index] >= \$start \&\&
${$probes_small{$chr}}[$index] <= $stop) {
            if ($stop - \$start >= \$size cutoff) {
$cnv_map_small{$patient}{$chr}{${$probes_small
                                    {$chr}}[\$index]} = \$type * 2;
}
else {
$cnv_map_small{$patient}{$chr}{${$probes_small
                                    {$chr}}[\$index]} = \$type;
}
}
\$index++;
}
\$last_index = \$index;
}
}

# Done Mapping small CNV calls

# determine final truth values

foreach my \$chr (keys oprobes_small) {

```
```

for (my \$i = 0; $i < @{$probes_small{\$chr}}; \$i++) {
my \$position_small = ${$probes_small{$chr}}[$i];
if ($cnv_map_small{$patient}{$chr}{$position_small} > 1) {
if ($overlap{$patient}{$chr}{$position_small}
{\$gain_key} == 1) {
\$TP++;
}
else {
$FP++;
        }
    }
    elsif ($cnv_map_small{$patient}{$chr}{$position_small} <
            -1) {
        if ($overlap{$patient}{$chr}{$position_small}
            {$loss_key} == 1) {
\$TP++;
}
else {
$FP++;
        }
    }
    else {
        if (defined($overlap{$patient}{$chr}{$position_small}
            {$none_key}) \&\& $overlap{$patient}{$ch\overline{r}}
            {$position_small}{\$none_key} == 1) {
$TN++;
    }
        else {
            if (defined($overlap{$patient}{$chr}
{$position_small}{$large_key}) \&\&
$overlap{$patient}{$chr}{$position_small}
{$large_key} == 1) {
                # gain
                if (defined($overlap{$patient}{$chr}
{\$position_small}{gain_key}) \&\&
$overlap{$patient}{$chr}
                    {$position small}{gain key} == 1) {
if ($cnv_map_small{$patient}{$chr}
                    {$position_small} >= 1) {
\$TP++;
}
else {
$FN++;
                    }
                }
                # loss
                else {
                    if ($cnv_map_small{$patient}{$chr}
{\$position_small} <= -1) {
\$TP++;
}
else {
\$FN++;
}
}
}
else {
\$TN++;
}
}
}

```
```

                                    }
                }
            }
            # Probe output
            open(OUTFILE, ">>".$output_dir.$ratio_large.'_'.$output_type.$postfix.
                '.txt');
            print OUTFILE $ratio_large."\t".$ratio_small."\t".$TP."\t".$FP."\t".
            $TN."\t".$FN."\t".$discarded."\t".($TP+$FP+$TN+$FN+$discarded)."\n";
            close(OUTFILE);
    }
    }
print 'Analysis Complete!'."\n" unless \$quiet;

```

\section*{B. 2 Microsoft Excel Formatting Script}
```

\#!/usr/bin/perl

# Written by Corey Goodman - Electrical and Computer Engineering,

# University of Iowa

# THIS SCRIPT DEPENDS ON the Excel::Writer module

# 

use strict;
use warnings;
eval { require Excel::Writer::XLSX; 1 } or die required_module();
use Getopt::Long qw(:config gnu_getopt);
use Scalar::Util qw(looks_like_number);
sub required_module {
print 'Cānot use script because a dependant module is not installed'."\n";
print 'Excel::Writer module can be found at the following location'."\n";
print 'http://search.cpan.org/~jmcnamara/Excel-Writer-XLSX-0.05/'."\n\n";
usage();
}
sub usage {
print <<"USAGE";
Usage: perl \$0 [OPTIONS] <list_of_directories>
-o, --output Name of the output file placed in the same
directory as the result files. If not specified
default name is CombinedROCResults.xlsx
-a, --averages Normalize the true negatives (TN) using
the average CNV size if not specified the
TN rate is not normalized (optional)
-d, --directory Directory containing CNV call files
(required when using -a option)
Low resolution array type key used in
CNV call files in first column
(required when using -a option)
Flag used to suppress output while analysis is
running. If not specified script progress is printed
while running (optional)
-h, --help Print this message
IF AN EXISTING FILE IS SPECIFIED AS OUTPUT IT WILL BE OVERWRITTEN
format of CNV call file names:
[log2 ratio]_[filename].txt e.g. 0.30_CNVCalls.txt
Note: All files must end with a ".txt" extension and have UNIX line endings. The first line of all files is expected to be a header line and is not parsed out. The files are all tab delimitated with no quotation marks surrounding fields. On most UNIX platforms line endings can be converted with "dos2unix". Array type identifier for microarrays must be the same identifier specified in probe_roc.pl script

```
```

*When defining columns in files
rc = required column column must be present and meet formatting
standards set
uc = unimportant column column must be present but does not need to meet
any format standards
nc = non-required column column does not need to be present
format of CNV call files in each directory:
(Column Field Description [Field Format Descriptiion])
rcl: Sample name
Format: [patient unique id]_[array type identifier]
rc2: Genomic position
Format: [chromosome]:[start]-[stop]
Note: chromosome is in the format chr[XX] where XX is chromosome identifier
rc3: CNV event
Possibilities: Gain, Loss
uc4: CNV length
uc5: Cytoband
uc6: Probe log2 median
rc7: Number of probes
format of ROC analysis output file names:
[log2 ratio]_[analysis type]_Results.txt e.g. 0.30_Both_Results.txt
The analysis types possible are:
Both - Analysis includes deletions and duplications
Gain - Analysis includes duplications only
Loss - Analysis includes deletions only
format of files in list of directories:
(Only results files should be in the directories)
rc1: gold standard (higher resolution) log2 ratio
rc2: lower resolution log2 ratio
rc3: True Positives (TP)
rc4: False Positives (FP)
rc5: True Negatives (TN)
rc6: False Negatives (FN)
rc7: Discarded Probes
rc8: Total Probes
Notice: analysis including CNVs on the X/Y chromosome should be
interpreted with caution.
USAGE
exit;
}

# default set variables

my \$size cutoff = 400000;
my \$outfile = 'CombinedROCResults';
my \$gain_key = 'Gain';
my \$loss_key = 'Loss';
my \$both_key = 'Both';

# potential future feature

my \$derivitive = '';
my \$averages = '';
my \$directory = '';

```
```

my \$res_key = '';
my \$qui\overline{et = '';}
my $opt_ok = GetOptions(
    'a|averages' => \$averages,
    'q|quiet' => \$averages,
    'd|directory=s' => \$directory,
    'r|resolution=s' => \$res_key,
    'o|output=s' => \$outfile,
    'h|help' => sub { usage(); },
);
usage() unless ((@ARGV > 0) && (!$averages || \$directory));

# TN Column

my \$TN = 4;
my \$average_adjusted = 'Average_Adjusted';
my \$output_ext = '.xlsx';
my @analysis_files = ();
my %average_probes = ();
my %cnv count = ();
my %pro\overline{be_sum = ();}

# remove any path info if needed

my @out_split = split('/', \$outfile);
if (@out_split > 1) {
\$outfile = $out_split[@out_split-1];
}
if ($averages \&\& !($outfile =~ m/^($average_adjusted)/i)) {
\$outfile = $average_adjusted.'_'.$outfile
}

# append extension if needed

if (!($outfile =~ m/\.xlsx$/)) {
\$outfile .= '.xlsx';
}

# compute CNV averages if flag is set

if (\$averages) {
print 'Using average FPR adjustment'."\n" unless \$quiet;
opendir(MAIN_DIR, \$directory) or die 'Could not open directory: '.
\$directory." : \$!\n";
@analysis_files = readdir(MAIN_DIR);
\# read each file in CNV call file directory
foreach my $analysis_file (@analysis_files) {
            # ignore hidden files
            if(!($analysis file =~ m/^(\.)/i)) {
my \$file_ok = 1; \# true
\# check if filename meets analysis file naming standard
my @file_parts = split('_', \$analysis_file);
my \$log_ratio = $file_parts[0];
                if (looks_like_number($log_ratio)) {
$cnv_count{$log_ratio}{\$gain_key} = 0;
$cnv_count{$log_ratio}{\$loss_key} = 0;
$cnv_count{$log_ratio}{\$both_key} = 0;

```
```

$probe_sum{$log_ratio}{\$gain key} = 0;
$probe_sum{$log_ratio}{\$loss_key} = 0;
$probe_sum{$log_ratio}{$both_key} = 0;
open(IN, '< '.$directory.'/'.\$analysis_file);
my \$line = <IN>; chomp \$line; \# remove header line

# iterate over all CNV calls for ratio

while(\$line = <IN> ) {
chomp \$line; \# remove newline characters
\# double check file meets formatting standard
my @data_array = split("\t", $line);
    #turn line into an array of elements
    # stop if file irregularity
    if (!(($data_array[1] =~ m/^(chr)/i) \&\&
looks__like_number(\$data_array[6]))) {
\$file_ok = 0; last;
}
else {
my @sample_info = split('_', \$data_array[0]);
my \$call_type = $data_array[2];
        if ($sample_info[1] eq \$res_key \&\& \$data_array[3] >
\$si\overline{ze_cutoff) {}
$cnv_count{$log_ratio}{\$both_key}++;
$probe_sum{$log_ratio}{\$both_key} +=
$data_arrray[6];
                if ($call_type eq \$gain_key) {
$cnv_\overline{count{$log_ratīio}{\$gain_key}++;}
$probe_sum{$log_ratio}{\$gain_key} +=
$data arrray[6];
            }
                elsif ($call_type eq \$loss_key) {
$cnv_count{$log_ratio}{\$loss_key}++;
$probee_sum{$log_ratio}{\$loss_key} +=
\$data_array[6];
}
}
}
}

# compute averages if file_ok

if (\$file_ok) {
$average probes{$log ratio}{\$gain key} =
$cnv_count{$\log_ratio}{\$gāin_key} > 0 ?
$probe_sum{$log_ratio}{\$gain_key} /
$cnv_count{$log_ratio}{\$gain_key} : 1;
$average_prob\overline{es {$log_ra\overline{t}io}{\$loss_ke\overline{y}}=}=
$cnv_count{$log_ratio}{\$loss_key} > 0 ?
$probe_sum{$log_ratio}{\$loss_key} /
$cnv_count{$log_ratio}{\$loss_key} : 1;
$average_probes{$log_ratio}{\$both_key} =
$cnv_count{$log_ratio}{\$both_key} > 0 ?
$probe_sum{$log_ratio}{\$both_key} /
$cnv_count {$log_ratio}{\$both_key} : 1;
}
else {
warn 'A CNV call file may not be formatted correctly:
\$analysis_file."\n";

```
                                    }
                                    close(IN);
                }
        } # analysis dir
    }
    if (keys %average_probes < 1) {
        warn 'The files used to calculate the probe averages may not be '.
                            'formatted correctly'."\n";
    }
    closedir(MAIN_DIR);
}
# Loop through each directory
foreach my $dir (@ARGV) {
    if (substr($dir,-1,1) ne '/') {
        $dir .= '/';
    }
    print 'Compiling results in '.$dir."\n" unless $quiet;
    &read_data($dir, $outfile, \%average_probes);
}
```

\# Subroutine that reads all result files in a directory
\# and merges them into one excel workbook with multiple
\# sheets
sub read_data \{
my \$result_dir = shift;
my \$output-file = shift;
my \$reference = shift;
use vars qw (\$TN);
use vars qw (\$averages);
use vars qw(\$derivitive);
use vars qw (\$quiet);
use vars qw (\%average_probes);
my @additional_headers = ('FPR', 'Sensitivity', 'Distance to (0,1)',
'Optimāl Linear Ratio');
my @derivitive_headers = ('Normalized Slope', '\% Change in Slope', 'Derl',
'Der2', 'Optimal Der Ratio');
my @alphabet = ("A".."Z");
my \$workbook = Excel::Writer::XLSX->new( \$result_dir.\$outfile );
\# read all result files in directory
opendir(RESULT_DIR, \$result_dir) or die 'Could not open directory: '.
\$result_dir." : \$! \n";
my @result_files $=$ readdir (RESULT_DIR);
foreach my ${ }^{-}$\$result_file (@result_files) \{
\# ignore hidden files
if(! (\$result_file $=\sim \mathrm{m} / \wedge(\backslash) / i$.$) ) \{$
\# check if filename meets analysis file naming standard
my @file_parts = split('_', \$result_file);
my \$log_ratio = \$file_parts[0];
if (looks_like_number(\$log_ratio)) \{
my \$analysis_type = \$file_parts[1];
my \$no_common = (\$file_parts[2] =~ m/common/i) ?
' No Commmon' : '';
open(IN, '< '.\$result_dir.'/'.\$result_file);

```
my $worksheet_name = $log_ratio.' '.$analysis_type.$no_common.
    ' Analysis';
my $worksheet = $workbook->add_worksheet($worksheet_name);
my $bold = $workbook->add_format( bold => 1 );
# read file into array
my @data;
my $count = 0;
my $line = <IN>; chomp $line; # remove header line
my @headers = split("\t", $line);
#turn line into an array of elements
while($line = <IN> ) {
    chomp $line;
    my @data_array = split("\t", $line);
    #turn line into an array of elements
    for (my $n = 0; $n < @data_array; $n++) {
        $data[$n][$count] = $data_array[$n];
        }
        $count++;
}
close(IN);
# adjust averages if it has been specified
if ($averages) {
    for (my $i = 0; $i < @{$data[0]}; $i++) {
        if ($average_probes{$log_ratio}{$analysis_type}) {
                    my $old_count = $data[$TN][$i];
                        $data[$TN][$i] = int(($data[$TN][$i] /
                            $average_probes{$log_ratio}
                                    {$analysís_type}) + \overline{0.5);}
                # add to discarded probes
                $data[$TN+2][$i] += ($old_count - $data[$TN][$i]);
                # adjust new total probes
                $data[$TN+3][$i] -= ($old_count - $data[$TN][$i]);
            }
    }
}
$worksheet->write( 'A1', \@headers, $bold );
$worksheet->write( 'A2', \@data );
$worksheet->write( $alphabet[@headers].'1',
            \@additional_headers, $bold );
if ($derivitive) {
    $worksheet->write( $alphabet[@headers+@additional_headers].
                    '1', \@derivitive_headers, $bold );
}
my $max_row = @{$data[0]} + 1;
my $col = @data;
# Write equations to Excel sheet
for (my $row = 2; $row <= $max_row; $row++) {
    # (I) FPR
    $worksheet->write( $alphabet[$col].$row, '='.
                $alphabet[$col-5].$row.'/('.$alphabet[$col-4].
                $row.'+'.$alphabet[$col-5].$row.')' );
```

```
# (J) Sensitivity
$worksheet->write( $alphabet[$col+1].$row, '='.
        $alphabet[$col-6].$row.'/('.$alphabet[$col-3].
        $row.'+'.$alphabet[$col-6].$row.')' );
# (K) Linear Distance (normalized)
$worksheet->write( $alphabet[$col+2].$row, '=SQRT(()'.
        $alphabet[$col].$row.'/MAX('.$alphabet[$col].
        '$2:'.$alphabet[$col].'$'.$max row.'))^2) +(((MAX('.
        $alphabet[$col+1].'$2:'.$alpha\overline{b}et[$col+1].'$'.
        $max_row.')-'.$alphabet[$col+1].$row.')/MAX('.
        $alphabet[$col+1].'$2:'.$alphabet[$col+1].'$'.
        $max_row.')(^2))' );
# (L) Optimal using Line
$worksheet->write( $alphabet[$col+3].$row, '=IF('.
        $alphabet[$col+2].$row.'=MIN('.$alphabet[$col+2].
        '$2:'.$alphabet[$col+2].'$'.$max_row.'),'.
        $alphabet[$col-7].$row.',0)' );
if ($derivitive) {
    # (M) Normalized Slope
    if ($row < $max row) {
        $worksheet->write( $alphabet[$col+4].$row,
                            '=(((MAX('.$alphabet[$col+1].$row.','.
                                $alphabet[$col+1].($row+1).')-MIN('.
                                $alphabet[$col+1].$row.','.
                                $alphabet[$col+1].($row+1).'))*MAX('.
                                $alphabet[$col+1].'$2:'.$alphabet[$col+1].
                                '$'.$max_row.'))/(MAX('.$alphabet[$col].
                                $row.','.$alphabet[$col].($row+1).
                                ')-MIN('.$alphabet[$col].$row.','.
                                $alphabet[$col].($row+1).'))*MAX('.
                                $alphabet[$col].'$2:'.$alphabet[$col].
                '$'.$max_row.'))' );
    }
    # (N) Change in slope
    if ($row > 2 && $row < $max row) {
        $worksheet->write( $alp\overline{habet[$col+5].$row,}
                                '=(MAX('.$alphabet[$col+4].($row-1).','.
                                $alphabet[$col+4].$row.')-MIN('.
                                $alphabet[$col+4].($row-1).','.
                                $alphabet[$col+4].$row.'))/'.
                        $alphabet[$col+4].($row-1) );
    }
    # (O) Der1
    if ($row < $max_row) {
        $worksheet->write( $alphabet[$col+6].$row,
                        '=IF (ISERROR(('.$alphabet[$col+1].$row.'-'.
                        $alphabet[$col+1].($row+1).')/('.
                        $alphabet[$col].$row.'-'.$alphabet[$col].
                        ($row+1).')),10^100,('.$alphabet[$col+1].
                                $row.'-'.$alphabet[$col+1].($row+1).')/('.
                        $alphabet[$col].$row.'-'.$alphabet[$col].
                        ($row+1).'))' );
    }
    # (P) Der2
    if ($row < $max_row-1) {
        $worksheet->write( $alphabet[$col+7].$row,
            '=IF(ISERROR(('.$alphabet[$col+6].$row.
```

```
'-'.$alphabet[$col+6].($row+1).')/('.
$alphabet[$col].$row.'-'.$alphabet[$col].
($row+1).')),-1*10^100,('.
$alphabet[$col+6].$row.'-'.
$alphabet[$col+6].($row+1).')/('.
$alphabet[$col].$row.'-'.$alphabet[$col].
($row+1).'))' );
        }
        # (Q) Optimal using Der
        $worksheet->write( $alphabet[$col+8].$row, '=IF('.
                        $alphabet[$col+7].$row.'=MAX('.
                        $alphabet[$col+7].'$2:'.$alphabet[$col+7].'$'.
                        $max_row.'),'.$alphabet[$col-7].$row.',0)' );
    }
}
# =SUM(L2:L12)/COUNTIF(L2:L12,">0")
$worksheet->write($alphabet[$col+3].($max_row+1), '=SUM('.
            $alphabet[$col+3].'2:'.$alphabet[$col+3].$max_row.
            ')/COUNTIF('.$alphabet[$col+3].'2:'.$alphabet[$col+3].
            $max_row.',">0")' );
# =SUM(Q2:Q1\overline{2})/COUNTIF(Q2:Q12,">0")
if ($derivitive) {
            $worksheet->write($alphabet[$col+8].($max_row+1), '=SUM('.
                    $alphabet[$col+8].'2:'.$alphabet[$col+8].$max_row.
                    ')/COUNTIF('.$alphabet[$col+8].'2:'.
                    $alphabet[$col+8].$max_row.',">0")' );
}
# Make chart
my $chart = $workbook->add_chart(
        type => 'scatter',
        subtype => 'smooth_with_markers',
        embedded => 1
);
# Configure the chart series data
$chart->add_series(
    name - => 'ROC '.$log_ratio,
    categories => '=\''.$worksheet_name.'\'!$'.$alphabet[$col].
            '$2:$'.$alphabet[$col]-'$'.$max_row,
    values => '=\''.$worksheet_name.'\'!$'.
            $alphabet[$col+1].'$2:$'.$alphabet[$col+1].
            '$'.$max_row,
);
$chart->set_legend( position => 'none' );
    my $chart_type = ($analysis_type =~ m/$both_key/i) ?
            'All Types' : ($analysis type =~ m/$gain_key/i) ?
                    'Duplications' : 'Deletions';
# Add a chart title and some axis labels.
$chart->set_title ( name => 'ROC Curve '.$chart type.' '.
            $log_ratio.$no_common."\n".'(Average Adjusted FPR)' );
$chart->set_x_axis(
    name =>`',
    min => 0,
);
$chart->set_y_axis(
    name => 'Sensitivity',
    max => 1,
);
```

```
                # Insert the chart into the worksheet (with an offset).
                $worksheet->insert_chart( 'A'.($max_row+1),
                        $chart, 10, 10, 1.11, 1.43 );
                    }
        }
    } # end reading files
    closedir(RESULT_DIR);
}
```

